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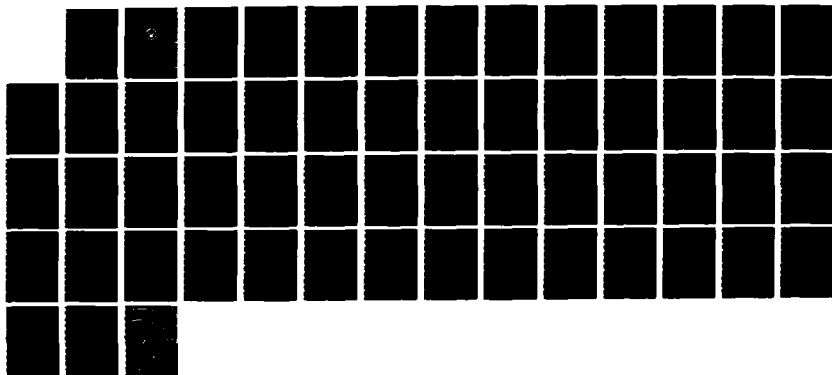
NUMERICAL COMPUTATION OF RING-SYMMETRIC SPACECRAFT
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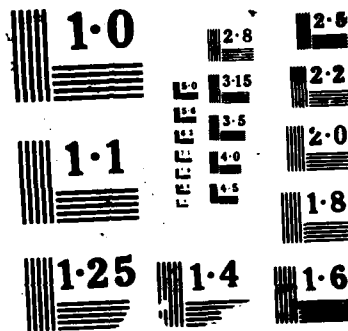
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CONTRACTOR REPORT

NUMERICAL COMPUTATION OF RING-SYMMETRIC
SPACECRAFT EXHAUST PLUMES

by

Joseph Falcovitz

January 1987

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Prepared for: Strategic Defense Initiative Office
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The work reported herein was performed for the Naval Postgraduate School by Dr. Joseph Falcovitz under contract N62271-86-M-0214. The work presented in this report is in support of "Rarefied Gas Dynamics of Laser Exhaust Plume" sponsored by the Strategic Defense Initiative Office/Directed Energy Office. This is a partial report for that contract. The work provides information concerning numerical computation of the flow in spacecraft exhaust plumes. The project at the Naval Postgraduate School is under the cognizance of Distinguished Professor A. E. Fuhs who is principal investigator.

Reproduction of all or part of this report is authorized.

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ABSTRACT

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NOMENCLATURE followed by units (if any) and CODE NOTATION (if any)

a	sound speed (m sec^{-1})
B	breakdown parameter [5,6,7]
C\pm	characteristic lines inclined at $(\theta \pm \mu)$
D	molecular diameter (hard spheres) (m)
M	Mach number
n	number density (molecules/ m^3)
p	pressure (Pa)
S	coordinate along streamlines (m)
u	flow velocity (m/sec)
x	axial cartesian coordinate
y	radial cartesian coordinate
γ	specific-heat ratio (G)
η	length coordinate along fan characteristics (C^+) (m)
θ	inclination of flow velocity vector
λ_0	mean free path at stagnation conditions (m)
μ	Mach angle ($\sin \mu = 1/M$) (MU)
v	Prandtl-Meyer function (NU)
ξ	length coordinate along transverse (C^-) characteristic
σ	collision cross-section πD^2 (m^2) (SIGMA)
τ	molecular opacity (expected number of collisions by a fast invading molecule) (XI)
ϕ	collision frequency (sec^{-1})
ω	symmetry index (0 - planar flow, 1 - axisymmetric flow) (DELTA)
Γ	the fraction $\left[(\gamma + 1)/(\gamma - 1) \right]^{1/2}$
(v + θ)	Riemann invariant along C^- (RM)
(v - θ)	Riemann invariant along C^+ (RP)

INDICES

()₀	a specific point in the CRW (x_0, y_0) (Also : stagnation conditions)
()₁	nozzle exit conditions
()_L	limiting CRW characteristic ($p = 0$)
()_f	final CRW characteristic (boundary of numerical integration)
()_c	corner of CRW

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1. INTRODUCTION

In a recent report [1] a mixed numerical/analytical approach to the computation of a ring-symmetric spacecraft exhaust plume was presented. The numerical scheme had been implemented in a code named "JET" which is capable of generating whole-plume flow fields, while the analytic approximation is restricted to the ring-symmetric centered rarefaction waves (CRW) that flank the plume. The present report is intended to serve as a supplement to [1] in providing details on the computational scheme and the code JET.

The spacecraft exhaust flow (Fig. 1 of [1]) is idealized as a ring-symmetric steady isentropic expansion of an ideal gas. The nozzle lips are assumed sharp; the supersonic flow from the exit surface of the ring-nozzle is assumed uniform, and the background is considered to be perfect vacuum.

The standard scheme for computing such idealized ring-plumes is the classical (direct) method of characteristics [2] . At a preliminary phase of the present laser exhaust study, a code AXSYM [3] was written for computing ring-plumes using this method. A notorious shortcoming of the direct method of characteristics is that the solution grid is highly irregular, being formed by the (oblique) intersection of the C^+ and the C^- families of characteristic lines. We first encountered a difficulty with this grid while seeking a scheme for integrating the molecular opacity along a straight line [1] . This computation would have required rather complex coding for the geometry of intersection between a straight line and an irregular grid. It seemed preferable to opt for a computation scheme that would produce a more regular grid, even at the expense of some loss of accuracy. Such scheme is the inverse marching method of characteristics [4] .

Generally the marching in this type of scheme is in the downstream direction, i.e., the y direction in our case. Grid points are located on a succession of constant- y rows, thereby introducing a measure of regularity in the solution grid. Just two rows have to be stored in the computer core memory - the "old" row and the "new" row, whereas in the direct method of characteristics whole grid-image matrices are required to reside simultaneously in core memory.

The first version of the JET code was based on the inverse marching scheme given by Zucrow and Hoffman (Section 12-5 in [4]), where the flow variables were the *two cartesian velocity components*. The computation seemed accurate everywhere, except within the centered rarefaction wave (CRW). In an attempt to replicate a planar CRW (Prandtl-Meyer flow), the numerical solution exhibited an

instability : Mach number increased along the (low pressure) boundary characteristic line, rather than remain constant.

A *qualitative* explanation for this instability is the following. Flow gradients in a CRW are inversely proportional to distance from the corner, so that the inverse marching scheme gives rise to an amplification of interpolation errors at every marching step, leading to an apparently divergent (unstable) numerical solution. Increasing the order of interpolation from linear to cubic did not eliminate the instability.

Looking for a scheme that would replicate a planar CRW accurately, we tried the modified marching idea as presented by Zucrow and Hoffman for 1-D time-dependent flows (Sections 19-6(a) and 19-6(j) of [4]). In this scheme new grid points are determined by forwardly extending a "primary" family of continuous characteristic lines from old grid points. The primary family in a CRW is the characteristics fanning out from the corner (we assume it is the C^+ family). By choosing this modified scheme, the interpolation for trace points obtained from reversely extended C^+ lines was eliminated. However, the corresponding interpolation for the transverse C^- characteristics remained, and with it the aforementioned instability.

In order to replicate a planar CRW, we had to replace the flow variables by the *Riemann invariants* ($v \pm \theta$). In a C^+ planar CRW, the Riemann invariant ($v + \theta$) is uniformly constant, so that the interpolation in ($v + \theta$) due to reversely extending C^- characteristics introduces no error at all. This scheme, which we named SIMA (Semi Inverse Marching Algorithm), was indeed verified to replicate a planar CRW exactly, when implemented in the code JET.

The plan of this report is the following. In Ch. 2 we supplement the description of the numerical scheme given in Ch. 2 of [1] , by adding more details on the computational procedure. A description of the code JET is given in Ch. 3, and the code listing is reproduced in Ch. 4.

Note on symmetry :

The code JET has two symmetry options. When DELTA = 1 a ring-symmetry is in effect; when DELTA = 0, a planar symmetry is in effect. An axisymmetric jet exiting in the y direction from the same nozzle aperture along the x axis can readily be computed by replacing all terms in the code that correspond to $\sin(\theta)/y$ in the compatibility equations (2.1-1), by $\cos(\theta)/x$. In that case the coding is virtually unchanged, and the only care that should be exercised is for the difference equations for new grid points on or near the y axis. Also, all reference to the analytic approximation of the ring-symmetric CRW [1] should be deleted in this case, as it is designed specifically for ring-symmetry.

2. THE COMPUTATIONAL SCHEME

A basic description of the semi inverse (SIMA) and inverse marching schemes was given in Ch. 2 of [1]. We supplement this description by specifying the slightly modified definition of Riemann invariants in the code, and by giving information about some ancillary computations.

2.1 Riemann Invariants

The compatibility equations whose integration constitutes the numerical solution to the governing equations [1] are expressed in terms of the Riemann invariants as follows :

$$\text{Along } C^+ \quad \dots \quad (v - \theta)_4 = (v - \theta)_2 + \omega \sin \mu_{24} \sin \theta_{24} \Delta \eta / y_{24} \quad (2.1-1)$$

$$\text{Along } C^- \quad \dots \quad (v + \theta)_4 = (v + \theta)_1 + \omega \sin \mu_{14} \sin \theta_{14} \Delta \xi / y_{14}$$

The Riemann invariants $(v \pm \theta)$ are modified for convenience, by adding a constant to both v and θ . The new definitions of $v(M)$ and θ are :

$$v(M) = -\Gamma \arctan(\Gamma q) + \arctan(q)$$

$$q = (M^2 - 1)^{-1/2} \quad (2.1-2)$$

$$\theta \rightarrow \theta - \theta_L$$

Thus, in a Prandtl-Meyer flow with entry Mach number of M_1 , the modified values of both $v(M)$ and θ vanish as $M \rightarrow \infty$. As a consequence, in a C^+ Prandtl-Meyer flow the modified invariant $(v + \theta)$ vanishes uniformly. In this modified form, the computation of M from $v(M)$ is readily done by performing standard Newton-Raphson iterations (in RFUNC), using the derivative :

$$v'(q) = -(\Gamma^2 - 1) [(1 + \Gamma^2 q^2)(1 + q^2)]^{-1} \quad (2.1-3)$$

2.2 The Integration Scheme for a New Grid Point

The integration scheme has been sketched in Ch. 2 of [1] . It is performed in INVMAR for inverse marching points or in SEMINV for semi-inverse marching (SIMA) points. The computational scheme is specified via the following seven-step procedure :

INVMAR (Inverse Marching)

- (a) Grid : At this stage the new grid point has already been defined.
- (b) Predictor : Flow variables are the interpolated (linear nearest-neighbor) value on the old row for a point having the new grid x coordinate (x_4).
- (c) Centered variables : Denote the Riemann invariants by

$$RM = (v + \theta) \quad (2.2-1)$$

$$RP = (v - \theta)$$

then centered values for segments (1,4) and (2,4) (using code notation) are :

$$\begin{aligned} RM_{14} &= (RM_1 + RM_4)/2 & RP_{14} &= (RP_1 + RP_4)/2 \\ RM_{24} &= (RM_2 + RM_4)/2 & RP_{24} &= (RP_2 + RP_4)/2 \end{aligned} \quad (2.2-2)$$

All other centered flow variables are computed from the centered Riemann invariants by calling RFUNC.

- (d) Inverse Extension : old trace points x_1, x_2 are evaluated from the geometrical relations

$$\text{Along } C^- \quad \dots \quad y_{\text{new}} - y_{\text{old}} = (x_4 - x_1) \tan(\theta_{14} - \mu_{14}) \quad (2.2-3)$$

$$\text{Along } C^+ \quad \dots \quad y_{\text{new}} - y_{\text{old}} = (x_4 - x_2) \tan(\theta_{24} + \mu_{24})$$

- (e) Interpolation : find Riemann invariants RM, RP at old trace points x_1 and x_2 through nearest-neighbor linear interpolation by calling INTERP.
- (f) Integration : Using the compatibility relations in finite-difference form (2.1-1) with segment-centered coefficients, compute iteration-updated values of Riemann invariants at new grid point.

- (g) Corrector : if values of Riemann invariants and old trace points x_1 , x_2 are not sufficiently convergent, resume the procedure at step (c) above.

SEMINV (Semi Inverse Marching - SIMA)

- (a) Grid : New grid point (x_4) is determined as part of the SIMA scheme at step (d) below.
- (b) Predictor : Flow variables are those of point (x_2, y_{old}).
- (c) Centered variables : Identical to step (c) above.
- (d) Semi-Inverse Extension : new grid point x_4 and old trace point x_1 are evaluated from the geometrical relations in Eq. (2.2-3) above.
- (e) Interpolation : find Riemann invariants RM, RP at old trace point x_1 through nearest-neighbor linear interpolation by calling INTERP.
- (f) Integration : Identical to step (f) above.
- (g) Corrector : Identical to step (g) above, except for replacing x_2 in the convergence test by x_4 .

2.3 Boundary Conditions

On the vacuum side the boundary conditions ($p=0$) can only be approximately implemented in a method of characteristics scheme. We do so by ending the computation on a certain "final" C^+ fan characteristic line that starts out with a sufficiently high Mach number M_f at the corner (typically $M_f=34$). The marching computation of new grid points on the boundary C^+ characteristic via the SIMA scheme is identical to that of C^+ characteristics within the ring-symmetric CRW. It is noted that under this boundary scheme some outflow takes place through the boundary characteristic line, so that the total mass flow through a row $y = y_{new}$ decreases slightly as y_{new} increases.

At the nozzle exit the boundary conditions are assumed to be uniform outflow in the radial (y) direction with Mach number M_1 . At the nozzle lip, the SIMA integration starts out from a presumed planar CRW (Prandtl-Meyer flow) at the corner (i.e., the associate CRW in the terminology of Ch. 3 in [1]).

At the plane of symmetry ($x=0$) the boundary condition is simply $\theta = \pi/2$. However, this condition is implemented indirectly, by assuming that the flow at virtual grid points with $x < 0$ is a mirror-image of the flow at the corresponding $x > 0$ points. The reason is that when a new grid point of $x_4 = 0$ or of x_4 sufficiently close to zero is considered for inverse-marching integration, the inversely extended trace point (x_1, y_{old}) can be at $x < 0$. Considering the subtraction of θ_L from θ as in Eq.(2.1-2), the reflection rules are :

$$RM \rightarrow RP + (\pi - 2\theta_L)$$

(2.3-1)

$$RP \rightarrow RM - (\pi - 2\theta_L)$$

where values on the left and right of the \rightarrow symbol correspond to values left and right of $x=0$. This boundary condition is implemented in INTERP.

2.4 Continuum Breakdown Surface

As an informative option, the code JET can compute (in PLUMES) points on a surface of continuum breakdown [5,6,7], which is defined as a line of constant B , where B is given by :

$$B = -(u/\varphi) \rho^{-1} (d\rho/dS)$$

(2.4-1)

$$\varphi = 4(\pi\gamma)^{-1/2} \sigma n a$$

When the standard isentropic relations for ρ and n in terms of M are substituted in (2.4-1), the flow speed is expressed as $u=Ma$ and the streamwise gradient of M is expressed in cartesian coordinates, we get :

$$B = \lambda_0 (\pi\gamma/8)^{1/2} M^2 \left[1 + ((\gamma-1)/2)M^2 \right]^{1/(\gamma-1)-1} [M_x \cos\theta + M_y \sin\theta]$$

(2.4-2)

$$\lambda_0 = (2^{1/2} \sigma n_0)^{-1}$$

Note that the sign of B has been chosen as positive for expansion flows. This definition is preferred to taking an absolute value of the flow gradient, since it assures proper interpolation of B even if its spatial distribution goes through $B=0$.

Due to the dependence of B on a spatial gradient, its numerical evaluation (see BREAK) is attributed to mid-grid points both in x and in y .

3. THE JET CODE

In this chapter we provide a concise description of the JET code according to its version at the time of the JET018 run. This description is intended as an aid in reading the code listing which is given in Ch. 4.

The plan of this chapter is as follows. Array variables that constitute the mainstay of the computational scheme are described in Section 3.1. Auxiliary array variables that are used primarily for processing the information generated by the numerical scheme, are described in Section 3.2, followed in Section 3.3 by a list of major parameters that control the computation (some of them also serve as run data). Finally, all subroutines are listed and described in Section 3.4.

3.1 Main Variables

The array variables used for the computational scheme are organized in two labeled COMMON groups. The first group /VECS/ is designed to hold two grid rows - the old row designated by suffix F and the new row designated by suffix N. The second group /CHARAC/ are characteristic-indexed arrays that hold information about continuous characteristic lines. This characteristic information is used in two ways : it is incorporated in the SIMA computational scheme for the CRW region, and it is used to store data for optional plotting of characteristic lines (see PLUMES and PRINT).

The basic organization is that the new arrays (suffix N) are those in which values are stored during the course of the marching computational procedure. At the end of each marching step, values are transferred from new arrays to old arrays (suffix F); this is done in MOVE. In the array listing below, we indicate in parenthesis the subroutine (or subroutines) in which that new array is defined.

/VECS/

XN(I)	x coordinate of grid point I. (GRIDN)
RMN(I)	modified Riemann invariant ($v + \theta$) at grid point I. (BEGIN, INVMAR, LOADC).
RPN(I)	modified Riemann invariant ($v - \theta$) at grid point I. (BEGIN, INVMAR, LOADC).
MN(I)	Mach number at grid point I (BEGIN, INVMAR, LOADC).
MUN(I)	Mach angle μ at grid point I. (BEGIN, INVMAR, LOADC).
TETAN(I)	true (unmodified) flow angle θ at grid point I. (BEGIN, INVMAR, LOADC).

BN(I) value of breakdown parameter B at point $I-1/2$ (and at half a marching step back in y as well). (BREAK).

XTEMP(I) used for auxiliary computation of $I-1/2$ grid points in PLUMES.

/CHARAC/

XCHARN(KC) x coordinate of point on characteristic line number KC. (BEGIN, SEMINV, PLUMES).

YCHARN(KC) y coordinate of point on characteristic line number KC. (BEGIN, SEMINV, PLUMES).

RMCHARN(KC) modified Riemann invariant $(v + \theta)$ of point on characteristic line number KC. (BEGIN, SEMINV).

RPCARN(KC) modified Riemann invariant $(v - \theta)$ of point on characteristic line number KC. (BEGIN, SEMINV).

TCHARN(KC) true (unmodified) flow angle θ at point on characteristic line number KC. (BEGIN, SEMINV).

MUCARN(KC) Mach angle μ at point on characteristic line number KC. (BEGIN, SEMINV).

CSIGNN(KC) sign of characteristic line number KC. It has value 1 for C^+ and value -1 for C^- . Note that upon reflection of a C^+ line from the symmetry plane ($x=0$), the sign value is changed from 1 to -1 . (BEGIN, SEMINV).

MCHARN(KC) Mach number at point on characteristic line number KC. (BEGIN, SEMINV).

MCHARI(KC) Mach number at Prandtl-Meyer's fan characteristic number KC at the corner. It is defined initially and is not changed during the run. (BEGIN).

3.2 Auxiliary Variables

In addition to the major arrays mentioned above, there are several groups of auxiliary arrays that do not affect the computational scheme, but are intended for informative processing of the results. These groups are /PLUME/, /IPLUME/, /THICKY/, /THICKX/, /GRP/. /PLUME/ is used to preserve points on special lines for later plotting (in a separate code). /THICKY/ and /THICKX/ are for storing values of radial (y) and lateral (x) molecular opacities. The group /GRP/ is used in conjunction with comparative computation of the ring-symmetric CRW flow according to the analytic approximation [1].

/PLUME/ (PLUMES, PRINT)

XPL(J,IPL) x coordinate at marching step J of special line number IPL.

YPL(J,IPL) y coordinate at marching step J of special line number IPL.

/IPLUME/ (PLUMES, PRINT)

KPL number of special lines computed in PLUMES.

ITYPL(IPL) index indicating the type of special line number IPL.

/THICKY/ (OPACY, PRINT)

XTH(J) x coordinate on boundary characteristic line at marching step J, from which radial opacity is integrated.

TH(J) radial opacity computed by y-integration from the boundary point defined by XTH(J) (up to current YN).

/THICKX/ (OPACX, PLUMES, PRINT)

YXI(JXI) y coordinate of printed row number JXI (the index JXI counts just rows that have been printed). The row to be printed next upon calling PRINT is the row having YF near YXI(JXI).

XI(I,JXI) lateral (x) molecular opacity [I] at point XF(I), for printed row JXI. It is obtained by numerically integrating the solution obtained from the JET computation (see OPACX).

XIPM(I,JXI) same as XI(I,JXI) except that the Prandtl-Meyer solution is used to estimate the flow at grid points XF(I).

XIGRP(I,JXI) same as above, except that the analytic approximation to a ring-symmetric CRW [I] is used to estimate the flow at grid points XF(I).

XIAPP(I,JXI) same as XIGRP(I,JXI) except that the numerical integration is replaced by an approximate closed-form expression [I] .

XIF(I,JXI) stores grid points XF(I) of printed row JXI.

/GRP/ (PRINT, HMSET, MFUNC, HINTER, MATCH)

DMINV increment of inverse Mach number for array MHINV(I).

MHINV(I) inverse Mach number array (from 0 to 1/MEXIT), from which the H(M) function can be evaluated (HMSET).

HMV(I) values of the H(M) function evaluated by numerical integration. It is used to compute this function by interpolation. (HMSET, HINTER).

3.3 Major Parameters

Parameters that define and control a particular run (such as the maximum y for the marching computation, the number of grid points on a row and many more) are defined in INIDAT. (The code JET has no input file and no READ statements). The major control parameters are grouped in /PAR/ (floating point) and in /IPAR/ (integers); thermodynamic data are grouped in /STAG/.

We indicate in the listing the subroutines in which the labeled COMMON group or a particular parameter is defined (or sometimes referred to).

/PAR/ (INIDAT)

MEXIT	nozzle exit Mach number (M_1).
MFIN	Mach number of the final (boundary) CRW characteristic at the corner (M_p).
YMAX	maximum value of y for the marching scheme. When YF.GE.YMAX the run is terminated.
DY0	initial marching step.
DY	current marching step.
DYNEXT	next marching step (YSTEP).
STAB	stability coefficient for marching step (STAB.LE.1). (See YSTEP).
DELTA	symmetry index. DELTA = 0 for plane symmetry; DELTA = 1 for ring-symmetry.
PSI1	angle of Prandtl-Meyer fan characteristic at exit conditions (measured from x axis).
PSIF	angle of final (boundary) Prandtl-Meyer fan characteristic.
SIGMA	collision cross-section (σ).
FRACG	the number of intervals initially allocated to the CRW fan is a FRACG fraction of the total number of intervals (KF0-1). (see BEGIN).
EPSIL	convergence parameter (small number). (INVMAR, SEMINV).
TETLIM	flow angle (from x axis) of the limiting ($p = 0$) velocity vector of the flow at the lip-centered Prandtl-Meyer fan.
TETSYM	PAI-2*TETLIM for reflection transformation (see INTERP).

/IPAR/ (INIDAT)

JMAX	maximum number of marching steps. If J.GE.JMAX run is terminated.
KF0	initial (and maximum) number of grid points in a row.
KF	current number of grid points in the old row.
KN	current number of grid points in the new row.

ITER0 maximum number of iterations for the integration of the compatibility relations
 (see INVMAR and SEMINV; also used in RFUNC, PLUMES).
 IM, IP search indices for interpolation subroutine INTERP. (see INVMAR, SEMINV).
 J current row index (also index of a marching step).
 KF2 defined as $2 \cdot KF$; not used in present version.
 IDEL, JDEL increments for printing grid point I and row J (see PRINT).
 JYXI number of rows to be printed in a run.
 JXI index of printing row, to be printed next (see PRINT).
 ILEAD index I at the first grid point on current new row, where the SIMA integration
 commences. Initially this point corresponds to the leading characteristic of the
 CRW. (see GRIDN, BEGIN).
 ILEADF value of ILEAD for current old row.
 KCLEAD index in the characteristic array for the characteristic line that corresponds to the
 new grid point $I = ILEAD$ (see GRIDN). Initially $KCLEAD = 1$.

/STAG/ (INIDAT)

RHO0, N0 stagnation density and number density.
 P0, T0, A0 stagnation pressure, temperature and sound speed.
 MDOT1 mass flow rate from ring-nozzle (only from the $x > 0$ half). (See PRINT).

/ICHARA/ (BEGIN)

KCHARP number of C^+ characteristic lines for which data is stored (either for SIMA
 computation or for subsequent plotting).
 KCHARM number of C^- characteristic lines for which data is stored (only for subsequent
 plotting).
 KCHAR0 total number of characteristics for which data is stored, i.e.,
 $KCHAR0 = KCHARP + KCHARM$.

3.4 Description of JET subroutines

MAIN PROGRAM

The main program performs two functions. The first section (up to statement 1) is the initial set up; it is performed just once. The second section is the marching loop with the step index J. This program can be read as a flow chart of the overall computational procedure.

INIDAT is for setting up run data. In BEGIN the initial conditions for the marching computation are set up. A single marching step is performed by calling MARCH, and the loading of new row vectors into old row vectors is done by calling MOVE. The call to YSTEP is for the first computed marching step. All remaining calls are for informative tasks (see HMSET, BREAK, OPACY, PLUMES, PRINT). Run is terminated when either YF.GE.YMAX or when J.GE.JMAX.

NOTE ON EXEC: The only special feature in the EXEC is retaining the output unit 7 file for optional post-plotting. The printed output (unit 6) is the system's standard (default).

INIDAT

Initial data definition and preliminary data computations. The data is defined by statements rather than by reading an input file. The meaning of major parameters was described in Section 3.3 above. User is invited to modify the data definitions, particularly of run-control parameters such as YMAX, JYXI and YXI(JXI) (for printing JYXI selected rows).

BEGIN

Here all initial values (prior to beginning of marching schemes integration) are loaded into all major computational arrays (Section 3.1). Also, values of the key integer parameters KCHARP, KCHARM, KCHAR0, ILEAD, KCLEAD and KF are defined.

In the first loop (loop 1) we define an initial family of C^+ characteristic lines for the lip-centered CRW, by storing the Mach number of the Prandtl-Meyer fan characteristics in the array

MCHARI(KC). Note that the fan characteristics are generated at equal RP intervals, since the flow variables are RM and RP. However, a different division might also be acceptable.

The next step is the definition of initial values for all characteristic arrays, first the C^+ arrays (loop 2), then the C^- arrays (loop 21). The C^- characteristic lines are needed just for informative output (post-plotting), so the present version contains just one C^- line. The user may modify that.

The remaining grid points (altogether KF0 grid points are initially available) are uniformly distributed across the nozzle opening, and the row arrays are loaded with the corresponding nozzle-exit flow variables (loop 3).

PRINT

The main task of this subroutine is the printing of flow variables at grid points of selected rows. The printing of a row is selected when YF is close to a predefined array YXI(JXI). Following the printing, JXI is updated by adding 1.

For comparison, additional flow variables are printed for each row. These are computed from the analytic approximation to a ring-symmetric CRW [1], by calling MATCH. Also, lateral molecular opacities of various kinds of approximation are computed by calling OPACX, and are printed for each grid point within the CRW.

Following the row printing (statement 120), arrays intended for post-processing (plotting of special lines) are printed and subsequently written on output unit 7. This is done once per run, just before run termination.

FIN

This subroutine is called when an error is encountered, in order to terminate the run. Note that the run is terminated by deliberately introducing an error of computing $\text{SQRT}(-1)$, which is done in order to trigger the printing of calling sequences by the operating system.

MARCH

This subroutine performs a single marching step by calling the proper computational subroutines at an appropriate sequence. It can be read as a flow chart of the entire computational scheme. First the segment of the new row suitable for SIMA computation is calculated by calling SEMINV. Then new grid points for that part of the new row for which inverse marching integration is to be performed, are generated by calling GRIDN. The results of the SEMINV computation, which were stored in characteristic arrays, are now loaded into row arrays by calling LOADC. Finally, the computation of the new row is completed by calling INVMAR which computes the flow at the remaining grid points by the inverse marching scheme.

INVMAR

This is one of the two central subroutines for computing the flow at new grid points (the other is SEMINV). Here the inverse marching scheme is used. The computational procedure follows the seven-step description given in Section 2.2 above. Note that the initial value of the search indices IM and IP is not redefined at each call to INTERP, since it is assumed that IM and IP do not change much at consecutive calls to INTERP, so that search efficiency is enhanced by not starting the search from an arbitrary point (such as either end of the row).

SEMINV

This is the subroutine performing the SIMA scheme for computing the flow at new grid points located along continuous characteristic lines of the lip-centered CRW (at prescribed y-marching steps). The essence of the computational procedure of this subroutine was given as a seven-step description in Section 2.2. The same remark about IM given in the preceding INVMAR description applies here as well.

The main loop (100) is over all characteristic lines, including some C^- lines in addition to the C^+ lines. Thus, the array CSIGNF(KC) is used to get the appropriate expressions for either C^+ or C^- characteristics. It is noted that while normally the characteristic segments through points 1 and 2 are C^- and C^+ respectively, this is reversed when a C^- rather than a C^+ line is computed via the SIMA scheme. In this case, which is characterized by having CSIGNF(KC).LT.0, the Riemann

invariants integrated along segments (1,4) and (2,4) are interchanged. This is done in the few statements just preceding and following statement 21.

An additional capability of this subroutine is to treat a change of a C^+ characteristic line into a C^- line upon reflection from the symmetry plane ($x=0$). This is done by first computing a new grid point having $X4.LT.0$, and then changing its sign after setting $CSIGNN(KC) = -1$ (statements just preceding statement 30). It is also possible to skip the computation of a particular characteristic by setting $CSIGNN(KC)=0$. This feature is not exploited in the present version.

Finally, we note that not all characteristic lines computed here are part of the marching flow computation. Only those with indices KC between $KCLEAD$ and $KCHARP$ are. All other characteristic lines are computed just for informative purposes (post-plotting).

RFUNC

Here M , MU , $TETA$ are computed from the two Riemann invariants RM , RP . The computation of M is performed by a Newton-Raphson iteration using Equations (2.1-2) and (2.1-3) given in Section 2.1 above.

INTERP

This subroutine starts by finding through a search procedure the grid interval ($I, I+1$) that contains a given point X . Then the Riemann invariants are computed for this point by linear interpolation, and returned in RM , RP . Note that X may be negative, which accounts for the relatively elaborate search logic in the determination of I , and for the reflection transformation (as in Eq. (2.3-1) above) preceding the last two statements of the subroutine.

INTERX

This interpolation routine performs an inverse task to that of `INTERP`, in that it finds the point $X0$ that corresponds to a given linearly interpolated value of the flow variable $VAR0$. It is used in `PLUMES` to compute the location of a breakdown surface point on a new row of x -centered and y -centered grid points

BREAK

This subroutine computes the new breakdown parameter array $BN(I)$. The computation is based on the description given in Section 2.4 above.

OPACY

Here the radial (Y) molecular opacity array $TH(J)$ is computed. At each marching step J , a new boundary grid point $XTH(J)$ is added, then the radial opacities at all preceding boundary points are updated by adding the contribution of the gas layer between the current old and new rows. Note that since grid points on adjacent rows are not located on equal- X columns, this procedure requires X -interpolation by calling `INTERP`.

PLUMES

This is a user-defined subroutine, where up to 10 special lines can be computed and subsequently retained on output unit 7 for post-processing (plotting). The type of the line $ITYPL(IPL)$ and a parameter $VPL(IPL)$ that defines the line, are computed through user-inserted statements in the section preceding statement 2000. Then an additional point on the current new row is computed for each line type. The available types are clearly stated in comments. Note that characteristic lines have already been computed in `SEMINV` using the `SIMA` scheme, regardless of whether they are part of the solution grid to the flow field, or are just computed for informative purpose. It is the user's choice which of these lines (if any) are to be saved in the `/PLUME/` arrays for subsequent post-processing (plotting).

GRIDN

This subroutine computes the grid points in that segment of the new row for which the flow is computed by the inverse marching scheme (in `INVMAR`). Initially, this segment extends from $x=0$ to the new row grid point which lies on the leading characteristic of the lip-centered CRW. However, since the leading characteristic is reflected from the symmetry plane ($x=0$) at some point, this segment steadily shrinks in size as the marching proceeds. The remedy is to declare the next-to-the-

leading characteristic line ($KC = 2$) as the beginning of the segment for SIMA integration, by setting $KCLEAD = 2$. This process of increasing $KCLEAD$ is repeated whenever it is deemed necessary. The criterion in the present version for the minimal $KCLEAD$ is that the inverse-marching segment should be at least twice $DX1$ - the average CRW grid interval (loop 1, the two statements following $DX1 = \dots$). Also, $ILEAD$ is redefined for each row according to $XLEAD/DX1 + 2$ in order to achieve a row of relatively uniform grid intervals throughout. The result is that the number of grid points in a row is initially $KF0$, but eventually it decreases due to both increase of $KCLEAD$ and decrease of $ILEAD$.

YSTEP

In this subroutine the next marching step $DYNEXT$ is computed at the end of the current marching step. It is defined as the smallest step obtained by forward intersection of C^- and C^+ characteristics from adjacent grid points. Note that the actual value of $DYNEXT$ is reduced by a "stability" factor $STAB$, and that \dot{DY} is also limited by the growth-rate factor DDY and by $DYMAX$ (see MAIN PROGRAM).

MOVE

Here old row arrays (loop 1) and old characteristic arrays (loop 2) are loaded with values of flow variables from corresponding new arrays, in preparation for the next marching step. As a result of this organizational feature, informative computations (e.g. $BREAK$, $OPACY$) that require both new and old rows, have to be performed prior to calling $MOVE$.

OPACX

Here lateral (X) opacities that correspond to the number of expected collisions of a fast molecule invading the CRW in the $-X$ direction, are computed. All opacities, except $XIAPP(1)$, are computed by numerical integration. In loop 1 we compute the opacity contribution of the segment lying just outside the computational boundary characteristic ($MFIN$), assuming a Prandtl-Meyer flow. This additional opacity is denoted $XI0$. If the flow is ring-symmetric, $XI0$ is recalculated using the analytic approximation [1] to estimate the flow field at the fringes of the ring-symmetric CRW (see also the closed form expression for τ in [1]).

The computation of opacity arrays starts after statement 14. First, the opacity at each grid point is set to XI0. Thus, even though the numerical flow computation does not include the fluid outside the boundary characteristic line, the opacity integration includes an estimate of that "missing" part, i.e., of XI0. In typical case computations of a ring-symmetric CRW [1] we found that the maximum value of XI0 was about 0.16., which indicated that as far as interaction with invading ambient molecules is concerned, the approximation $MFIN = 34$ was a reasonable substitute for $MFIN = \infty$.

The next step is the computation by numerical integration of three approximations to the lateral opacity : XI(I,JXI), XIPM(I,JXI), XIGRP(I,JXI). (Note that when the flow is ring-symmetric, the approximation XIPM(I,JXI) obtained by assuming a Prandtl-Meyer flow is usually grossly exaggerated). The opacity XIGRP(I,JXI) is based on the analytic approximation to a ring-symmetric CRW [1] , and is reasonably close to XI(I,JXI) which is obtained from the numerical solution to the flow field. Finally, a simplified closed-form integration of lateral opacity [1] is computed as XIAPP(I,JXI) (loop 3). Thus, the quantitative difference between XI(I,JXI) and XIGRP(I,JXI) is an indication to the degree of accuracy achieved by the analytic approximation to a ring-symmetric CRW [1] , while the difference between XIGRP(I,JXI) and XIAPP(I,JXI) indicates the level of error introduced by the closed-form integration of lateral opacity [1] .

LOADC

Here flow variables of new grid points computed via the SIMA scheme (SEMINV) are loaded into new row arrays from corresponding characteristic arrays.

NUFUNC

This function computes the modified $v(M)$ value as given by Eq. (2.1-2). Note that presently $NU0 = 0$ (see INIDAT).

HMSET

This subroutine is called just once from the MAIN PROGRAM. Its task is to set up the arrays in /GRP/, so that the function $H(M)$ [1] can be evaluated by interpolation (in HINTER). There is also an informative printout of various derivatives (see Ch. 3 of [1]) generated in this subroutine.

MFUNC

This subroutine is called by HMSET in order to compute functions of Mach number that serve in the computation of $H(M)$. The output variable F is the integrand for the integration leading to $H(M)$.

HINTER

This subroutine computes $H(M)$ by linear interpolation in inverse Mach number, using the /GRP/ arrays computed in HMSET.

MATCH

This subroutine is called from PRINT to compute the Mach number according to the analytic approximation of a ring-symmetric CRW [1], for point $(YF, XF(I))$. $M0B$ is the associate Mach number $M(0, \beta)$, which is preserved in the array MCHARI(KC) for all CRW characteristics that are used in the SIMA computation. Hence the Mach number $M(\alpha, \beta)$, denoted by MAB can be computed directly from the analytic approximation [1] to the area function at $(YF, XF(I))$ by calling AREAF. Since typically $M(0, \beta)$ is not known, we also compute the Mach number via the inverse-problem procedure [1], denoting the resulting Mach numbers by suffix I: $M0BI$ for $M(0, \beta)$ and $MABI$ for $M(\alpha, \beta)$. The inverse-problem iterative procedure [1] is performed in loop 1, resulting in $M0BI$. From $M0BI$ the value of $MABI$ is computed through the area function approximation as for MAB above.

AREAF

This subroutine computes the Mach number M that corresponds to the area function F (Eq. (3.2-1) of [1]). The computation is done by Newton-Raphson iterations, and it has been found to converge when $M.GT.1$ (and when $M - 1$ is not much smaller than 1).

4. THE JET CODE LISTING

```

C#OPTIONS LIST
C JET018
C "JET" A SEMI-INVERSE MARCHING CHARACTERISTICS METHOD FOR RING JETS.
C USING RIEMANN INVARIANTS RM=(NU+TETA), RP=(NU-TETA) AS FIELD
C VARIABLES.
    IMPLICIT REAL*8(A-H,L-Z,*)
    REAL*4 XPL,YPL
    COMMON /PLUME/XPL(1002,10),YPL(1002)
    COMMON /IPLUME/KPL,ITYPL(10)
    COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1      TETA(101),BF(101),
2      XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3      TETAN(101),BN(101),XTEMP(101)
    COMMON/THICKY/XTH(1002),TH(1002)
    REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF
    COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)
1      ,XIAPP(101,20),XIF(101,20)
    COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1      G16,G17,G18,G19,G20
    COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2      TETSYN,TETLIM,DDY,DYMAX
    COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1
    COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1      KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
    COMMON /ROW/YF,YN,DXF,DXN
    COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),
1      RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),
2      TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),
3      CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),
4      MCHARI(92)
    COMMON /ICHARA/KCHARP,KCHARM,KCHARO
    COMMON /GRP/DMINV,MHINV(101),HMOV(101)
    COMMON /IGRP/KHM
C
101 PRINT 101
    FORMAT('1')
    J=1
    IF(J.EQ.1) STOP
    CALL INIDAT
    PRINT 101
    CALL HMSET
    PRINT 101
    CALL BEGIN
    CALL MARCH
    CALL OPACY
    CALL PLUMES
    CALL PRINT
    J=2
    CALL PLUMES
    CALL MOVE
    CALL OPACY
    CALL PRINT
    CALL YSTEP
    J=J+1
1
C DY WAS DETERMINED BY THE PREVIOUS CALL TO GRIDN.
    DY=DMINI(DYNEXT,DY*DDY,DYMAX)
C INTEGRATE BY ONE Y-STEP
    CALL MARCH
C BREAKDOWN PARAMETER (BF(I)).
    CALL BREAK
C SPECIALLY DESIGNATED LINES (FOR PLOTTING).
    CALL PLUMES
C STORE NEW LINE (N) IN OLD LINE (F).
    CALL MOVE
C COMPUTE RADIAL MOLECULAR OPACITIES
    CALL OPACY
C Y-STEP IS VARIABLE, SO JMAX IS USED AS END-OF-RUN CRITERION.
    IF(YF.GE.YMAX) JMAX=J
C PRINT FIELD AT MOST RECENT Y.
    CALL PRINT
C NEXT Y-STEP.

```

JET0001
 JET0002
 JET0003
 JET0004
 JET0005
 JET0006
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 JET0060
 JET0061
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 JET0063
 JET0064
 JET0065
 JET0066
 JET0067
 JET0068
 JET0069
 JET0070
 JET0071
 JET0072

CALL YSTEP	JET0073
IF(J.LT.JMAX) GO TO 1	JET0074
STOP	JET0075
END	JET0076
<hr/>	
SUBROUTINE INIDAT	JET0077
C SUBROUTINE NUMBER 1	JET0078
IMPLICIT REAL*8(A-H,L-Z,*)	JET0079
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET0080
1 TETAF(101),BF(101),	JET0081
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101),	JET0082
3 TETAN(101),BN(101),XTEMP(101)	JET0083
COMMON/THICKY/XTH(1002),TH(1002)	JET0084
REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF	JET0085
COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)	JET0086
1 ,XIAPP(101,20),XIF(101,20)	JET0087
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,	JET0088
1 G16,G17,G18,G19,G20	JET0089
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,	JET0090
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,	JET0091
2 TETSYM,TETLIM,DDY,DYMAX	JET0092
COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1	JET0093
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,	JET0094
1 KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD	JET0095
C COMMON /ROW/YF,YN,DXF,DXN	JET0096
PAI=4.D0*DATAN(1.D0)	JET0097
PAI2=2.D0*DATAN(1.D0)	JET0098
DEG=180.D0/PAI	JET0099
AR=8.3143D3	JET0100
AV=6.022D 26	JET0101
AW=7.27D0	JET0102
RH00=0.0075D0	JET0103
T0=2300.D0	JET0104
G=1.54D0	JET0105
D=2.5D-10	JET0106
MEXIT=4.D0	JET0107
MFIN=34.D0	JET0108
XC=0.5D0	JET0109
YC=2.5D0	JET0110
C DELTA=0 CORRESPONDS TO PLANE SYMMETRY	JET0111
C DELTA=1 CORRESPONDS TO CYLINDRICAL SYMMETRY	JET0112
DELTA=1.D0	JET0113
FRACG=0.6D0	JET0114
EPSIL=1.D-8	JET0115
ITER0=20	JET0116
KF0=101	JET0117
JMAX=1001	JET0118
STAB=0.50D0	JET0119
DDY=1.05D0	JET0120
DYMAX=0.5D0	JET0121
YMAX=50.D0	JET0122
DY0=YC/250.D0	JET0123
IDEL=1	JET0124
JDEL=1	JET0125
C POINTS FOR PRINTING FLOW FIELD AT YF=YXI(JXI)	JET0126
JXI=1	JET0127
JYXI=11	JET0128
DYXI=5.D0	JET0129
YXI(1)=YC+0.5D0	JET0130
YXI(2)=YXI(1)+2.D0	JET0131
I0=2	JET0132
DO 1 I=I0,JYXI	JET0133
YXI(I)=YXI(I0)+DYXI*DFLOAT(I-I0)	JET0134
1 CONTINUE	JET0135
IF(KF0.GT.101) CALL FIN(101)	JET0136
IF(JMAX.GT.1001) CALL FIN(102)	JET0137
IF(FRACG.GT.1.D0 .OR. FRACG.LT.0.) CALL FIN(103)	JET0138
IF(JYXI.GT.20) CALL FIN(104)	JET0139
IF(DELTA*(1.D0-DELTA).NE.0.) CALL FIN(105)	JET0140
NO=RH00*AV/AW	JET0141
A0=DSQRT(G*AR*T0/AW)	JET0142
P0=AR*RH00*T0/AW	JET0143
	JET0144

```

SIGMA=PAI*D**2
LAMDA0=1.D0/(DSQRT(2.D0)*SIGMA*N0)
G1=(G-1.D0)/2.D0
G2=(G+1.D0)/(2.D0*(G-1.D0))
G3=G/2.D0
G4=(G+1.D0)/(G-1.D0)
G5=DSQRT((G+1.D0)/(G-1.D0))
G6=1.D0/(G-1.D0)
G7=2.D0/(G+1.D0)
G8=(0.5D0*(G+1.D0)**2/(G-1.D0))*((1.D0/(G+1.D0))*
1 ((G+1.D0)/(G-1.D0))*((G-1.D0)/(G+1.D0))
G9=(G+3.D0)/(2.D0*(G-1.D0))
G10=(7.D0-3.D0*G)/(2.D0*(G-1.D0))
G11=(2.D0/(G+1.D0))*((1.D0/(G-1.D0))
G12=DSQRT((G+1.D0)/(G-1.D0))-1.D0
G13=(2.D0-G)/(2.D0*(G-1.D0))
G14=G/(2.D0*(G-1.D0))
G15=(G+1.D0)/(3.D0-G)
G16=(G+1.D0)/4.D0
G20=LAMDA0*DSQRT(PAI*G/8.D0)
ZETA1=G5*DATAN(DSQRT(MEXIT**2-1.D0)/G5)
AMU1=DARSIN(1.D0/MEXIT)
PSI1=PAI2+AMU1
ZETA1=G5*DATAN(DSQRT(MFIN**2-1.D0)/G5)
PSIF=PSI1+ZETA1-ZETA1
NU0=0.
TETLIM=NUFUNC(MEXIT)+PAI2-NU0
PSILIM=TETLIM
TETSYM=PAI-2.D0*TETLIM
GOREM=1.D0+G1*MEXIT**2
RH01=RH00/GOREM**G6
V1=MEXIT*A0/DSQRT(GOREM)
P1=P0/GOREM**((G/(G-1.D0))
T1=T0/DSQRT(GOREM)
YYC=2.D0*PAI*YC
IF(DELTA.EQ.0.) YYC=1.D0
MDOT1=YYC*XC*RH01*V1
C
PRINT 21,AR,AV,AW,G,RH00,N0,P0,T0,A0,D
21 FORMAT(/1X,'THERMODYNAMIC DATA: '/
1 1X,'AR,AV,AW,G=',2X,2D14.5,2F9.3/
2 1X,'RH00,N0,P0,T0,A0,D=',6D13.5)
PRINT 22,XC,YC,MEXIT,RH01,P1,T1,V1,MDOT1,PSI1*DEG,PSIF*DEG,
1 PSILIM*DEG
22 FORMAT(/1X,'CORNER DATA: XC,YC=',2F9.2/
1 1X,'EXIT CONDITIONS: ',
2 2X,'MEXIT,RH01,P1,T1,V1,MDOT1=',F9.3,5D13.4/
3 1X,'CENTERED FAN LIMITS: ',
4 2X,'PSI1,PSIF,PSILIM=',3F10.3)
PRINT 23,DELTA,KF0,JMAX,ITER0,DY0,YMAX,STAB,DDY
23 FORMAT(/1X,'INTEGRATION DATA. SYMMETRY INDEX: DELTA=',F4.1/
1 1X,'NUMBER OF POINTS IN X AND Y DIRECTIONS: KF0,JMAX=',
2 2I5/
3 1X,'MAX. NUM. OF ITERATIONS ITER0=',I5/
5 1X,'INITIAL Y-STEP AND MAXIMUM Y: DY0,YMAX=',2D14.5/
6 1X,'Y-STEP STABILITY FACTORS STAB,DDY=',2F7.3)
RETURN
END
SUBROUTINE BEGIN
C SUBROUTINE NUMBER 2
IMPLICIT REAL*8(A-H,L-Z,$)
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1 TETAF(101),BF(101),
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3 TETAN(101),BN(101),XTEMP(101)
COMMON/THICKY/XTH(1002),TH(1002)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1 G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,
2 TETSYM,TETLIM,DDY,DYMAX
COMMON /STAG/RH00,N0,P0,T0,A0,MDOT1

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BEGIN


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COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,          JET0217
1  KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD        JET0218
COMMON /ROW/YF,YN,DXF,DXN                            JET0219
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET0220
1  RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),      JET0221
2  TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),      JET0222
3  CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),      JET0223
4  MCHARI(92)                                          JET0224
COMMON /ICHARA/KCHARP,KCHARM,KCHARO                  JET0225
C  DEFINE INITIAL CHARACTERISTIC PARAMETERS. USE INTERPOLATION OF JET0226
C  RIEMANN INVARIANT ACROSS THE FAN.                  JET0227
C  KCHARP=IDINT(FRACG*DFLOAT(KF0-1)+1.D-6)+1         JET0228
KCHARO=KCHARP+1                                       JET0229
KCHARM=KCHARO-KCHARP                                 JET0230
IF(KCHARP.LT.2 ) CALL FIN(200)                        JET0231
IF(KCHARO.GT.92) CALL FIN(210)                        JET0232
IF(KCHARM.LT. 1) CALL FIN(205)                        JET0233
NU1=NUFUNC(MEXIT)                                    JET0234
RM1=NUO                                              JET0235
TET1=RM1-NU1                                         JET0236
RP0=NU1-TET1                                         JET0237
NUFIN=NUFUNC(MFIN)                                   JET0238
RPFIN=NUFIN-(RM1-NUFIN)                              JET0239
DRP=(RPFIN-RP0)/DFLOAT(KCHARP-1)                   JET0240
DO 1 KC=1,KCHARP                                    JET0241
RP1=RP0+DRP*DFLOAT(KC-1)                             JET0242
CALL RFUNC(RM1,RP1,M1,MU1,TETA1)                     JET0243
MCHARI(KC)=M1                                         JET0244
1  CONTINUE                                           JET0245
C  DATA FOR C+ CHARACTERISTICS.                      JET0246
C  THE RIEMANN INVARIANTS ARE DEFINED IN SUCH A WAY THAT BOTH VANISH AT JET0247
C  INFINITE MACH NUMBER.                             JET0248
RM1=NUO                                              JET0249
DO 2 KC=1,KCHARP                                    JET0250
CSIGNF(KC)=1.D0                                       JET0251
XCHARF(KC)=XC                                         JET0252
YCHARF(KC)=YC                                         JET0253
IF(MCHARI(KC).EQ.0.) CALL FIN(231)                   JET0254
NU=NUFUNC(MCHARI(KC))                                JET0255
TET=RM1-NU                                           JET0256
RP1=NU-TET                                           JET0257
CALL RFUNC(RM1,RP1,M1,MU1,TETA1)                     JET0258
MCHARF(KC)=M1                                         JET0259
MUCARF(KC)=MU1                                         JET0260
TCHARF(KC)=TETA1                                       JET0261
RMCARF(KC)=RM1                                         JET0262
RPCARF(KC)=RP1                                         JET0263
2  CONTINUE                                           JET0264
C  DATA FOR C- CHARACTERISTICS.                      JET0265
KC1=KCHARP+1                                         JET0266
XCHARF(KC1)=0.8D0*XC                                  JET0267
DO 21 KC=KC1,KCHARO                                  JET0268
CSIGNF(KC)=-1.D0                                       JET0269
MCHARI(KC)=MEXIT                                       JET0270
MUCARF(KC)=DARSIN(1.D0/MCHARI(KC))                   JET0271
TCHARF(KC)=PAI2                                       JET0272
YCHARF(KC)=YC                                         JET0273
MCHARF(KC)=MEXIT                                       JET0274
RMCARF(KC)=RM1                                         JET0275
RPCARF(KC)=NUFUNC(MEXIT)-(TCHARF(KC)-TETLIM)         JET0276
21 CONTINUE                                           JET0277
C  DEFINE GRID AND INITIAL CONDITIONS AT EXIT PLANE. JET0278
KFAN=KCHARP-1                                         JET0279
ILEAD=KF0-KFAN                                       JET0280
KCLEAD=1                                              JET0281
KF=KF0                                                JET0282
KF2=2*KF                                              JET0283
YF=YC                                                JET0284
DO 3 I=1,KF                                          JET0285
KC=KCLEAD+I-ILEAD                                    JET0286
IF(KC.GT.KCHARP) CALL FIN(241)                       JET0287

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IF(KC.GE.1) GO TO 31
XF(I)=DFLOAT(I-1)*XC/DFLOAT(ILEAD-1)
MF(I)=MEXIT
TETAF(I)=PAI2
GO TO 32
31 CONTINUE
XF(I)=XC
MF(I)=MCHARF(KC)
TETAF(I)=TCHARF(KC)
32 CONTINUE
RMF(I)=NUFUNC(MF(I))+(TETAF(I)-TETLIM)
RPF(I)=NUFUNC(MF(I))-(TETAF(I)-TETLIM)
MUF(I)=DARSIN(1.DO/MF(I))
BF(I)=0.
3 CONTINUE
DY=DY0
DO 4 KC=1,KCHAR0
CSIGNN(KC)=CSIGNF(KC)
4 CONTINUE
DO 5 I=1,KN
BN(I)=0.
5 CONTINUE
RETURN
END
PRINT
SUBROUTINE PRINT
C SUBROUTINE NUMBER 3
IMPLICIT REAL*8(A-H,L-Z,*)
REAL*4 XPL,YPL
COMMON /PLUME/XPL(1002,10),YPL(1002)
COMMON /IPLUME/KPL,ITYPL(10)
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1 TETAF(101),BF(101),
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3 TETAN(101),BN(101),XTEMP(101)
COMMON/THICKY/XTH(1002),TH(1002)
REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF
COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)
1 ,XIAPP(101,20),XIF(101,20)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1 G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,
2 TETSYN,TETLIM,DDY,DYMAX
COMMON /STAG/RH00,N0,P0,T0,A0,MDOT1
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),
1 RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),
2 TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),
3 CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),
4 MCHARI(92)
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1 KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
COMMON /ROW/YF,YN,DXF,DXN
C
SUM=0.
KF1=KF-1
DO 10 I=1,KF1
DX=XF(I+1)-XF(I)
GOREM=1.DO+G1*MF(I)**2
GOREM1=1.DO+G1*MF(I+1)**2
RATEM=RH00*A0*MF(I)*DSIN(TETAF(I))/GOREM**((G6+0.5D0)
RATEP=RH00*A0*MF(I+1)*DSIN(TETAF(I+1))/GOREM1**((G6+0.5D0)
SUM=SUM+DX*(RATEM+RATEP)/2.DO
10 CONTINUE
YYF=2.DO*PAI*YF
IF(DELTA.EQ.0.) YYF=1.DO
MDOTFR=YYF*SUM/MDOT1
PRINT 11, J,KCLEAD,KF,ILEAD,YF,DY,XF(KF),MF(KF),MDOTFR
11 FORMAT(1X,'J,KCLEAD,KF,ILEAD,YF,DY,XF(KF),MBOUND,MDOTR=',
1 4I5,5D12.4)
C
C PRINT FLOW FIELD AT Y=YF
C

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      IF(J.EQ.JMAX) JXI=MIN0(JXI,JYXI)
      IF(J.EQ.1 .OR. J.EQ.JMAX) GO TO 121
      IF(JXI.GT.JYXI) GO TO 120
      IF(YXI(JXI).GT.YF+0.5D0*DY) GO TO 120
121  CONTINUE
      YXI(JXI)=YF
      CALL OPACX
C  COMPUTE MACH NUMBER FOR CYLINDRICAL EXPANSION MCYL.
      F=(YF/YC)*(G7*(1.D0+G1*MEXIT**2))*G2/MEXIT
      CALL AREA(F,MCYL)
      PRINT 22,JXI,KCLEAD,ILEAD,KF,MCYL,YF
22  FORMAT(/1X,'PRINTING NUMBER  JXI,KCLEAD,ILEAD,KF=',4I4,
1    5X,'MCYL,YF=',2D14.5/)
      PRINT 1
1  FORMAT(/1X,'  I ', ' KC ', '      XF(I) ', ' TETAF(I) ',
      '      MF(I) ', ' MAB ',
2    '      MABI ', ' MOBI ',
3    '      XI(I) ', ' XIGRP(I) ',
4    '      XIAPP(I) ', ' XIPM(I) '/')
      IDEL1=IDEL
      IF(J.EQ.1.OR.J.EQ.JMAX) IDEL1=1
      DO 20 I=1,KF,IDEL1
      KC=KCLEAD+(I-ILEAD)
      IF(KC.LT.KCLEAD) KC=0
      MOB=1.D10
      MOBI=1.D10
      MAB=1.D10
      MABI=1.D10
      MPM=MF(I)
      IF(KC.EQ.0) GO TO 23
      MOB=MCHARI(KC)
      IF(J.EQ.1) GO TO 23
      PSIPM=PAI2-DATAN((XF(I)-XC)/(YF-YC))
      ZETA=PSI1+ZETA1-PSIPM
      MPM=DSQRT((G5*DTAN(ZETA/G5))*2+1.D0)
      CALL MATCH(I,MOB,MAB,MOBI,MABI)
23  CONTINUE
      PRINT 21,I,KC,XF(I),TETAF(I)*DEG,MF(I),MAB,MABI,MOBI,
1    XI(I,JXI),XIGRP(I,JXI),XIAPP(I,JXI),XIPM(I,JXI)
21  FORMAT(1X,2I4,10D12.4)
20  CONTINUE
      IF(J.EQ.1) GO TO 120
      IF(J.EQ.JMAX) GO TO 120
      JXI=JXI+1
120  CONTINUE
      IF(J.LT.JMAX) GO TO 200
      PRINT 101
101  FORMAT('1')
      PRINT 102
102  FORMAT(1X,'RADIAL MOLECULAR THICKNESS  J,XTH(J),TH(J)='/)
      PRINT 202,(JJ,XTH(JJ),TH(JJ),JJ=1,JMAX)
202  FORMAT(/5(I5,D11.4,D10.3))
      PRINT 101
      PRINT 103,(IPL,ITYPL(IPL),IPL=1,KPL)
103  FORMAT(1X,'PLUME TYPES  IPL,ITYPL(IPL)=' ,
1    2(/1X,5(5X,2I4)))
      PRINT 104
104  FORMAT(1X,'PLUME POINTS  J,YPL(J),XPL(J,1),XPL(J,2),...='/)
      JDEL1=1
      DO 203 JJ=1,JMAX,JDEL1
      PRINT 204,JJ,YPL(JJ),(XPL(JJ,IPL),IPL=1,KPL)
204  FORMAT(1X,I5,2X,E12.4,10E11.3)
203  CONTINUE
C  WRITE ON TAPE7 FOR SUBSEQUENT PLOTTING.
C  NO MORE THAN 80 CHARACTERS PER LINE ON TAPE7.
      WRITE(7,205) JMAX,KPL
205  FORMAT(8I10/8I10)
      WRITE(7,205) (ITYPL(IPL),IPL=1,KPL)
      DO 210 JJ=1,JMAX
      WRITE(7,211) YPL(JJ),(XPL(JJ,IPL),IPL=1,KPL)
211  FORMAT(6E13.6/2X,6E13.6/2X,6E13.6/2X,6E13.6)
210  CONTINUE

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C	WRITE LATERAL (X) OPACITIES	JET0433
	JXIO=JXI	JET0434
	WRITE(7,205) JXIO,KF0	JET0435
	PRINT 226, JXIO,KF0	JET0436
226	FORMAT(///1X,'LATERAL (X) OPACITIES JXIO,KF0=',2I8)	JET0437
	DO 220 JXI=1,JXIO	JET0438
	WRITE(7,221) JXI,YXI(JXI)	JET0439
221	FORMAT(I10,E13.6)	JET0440
	PRINT 227, JXI,YXI(JXI)	JET0441
227	FORMAT(//1X,'JXI,YXI(JXI)=' ,I8,E15.6/)	JET0442
	DO 225 I=1,KF0	JET0443
	WRITE(7,211) XIF(I,JXI),XI(I,JXI),XIPM(I,JXI),XIGRP(I,JXI),	JET0444
1	XIAPP(I,JXI)	JET0445
	PRINT 211, XIF(I,JXI),XI(I,JXI),XIPM(I,JXI),XIGRP(I,JXI),	JET0446
1	XIAPP(I,JXI)	JET0447
225	CONTINUE	JET0448
220	CONTINUE	JET0449
200	CONTINUE	JET0450
	RETURN	JET0451
	END	JET0452
	SUBROUTINE FIN(IFIN)	JET0453
C	SUBROUTINE NUMBER 4	JET0454
C	STOP WHEN ERROR IS DETECTED.	JET0455
	IMPLICIT REAL*8(A-H,L-Z,*)	JET0456
	PRINT 1,IFIN	JET0457
1	FORMAT(/1X,'FIN CODE IFIN=' ,I6/)	JET0458
C	INDUCE ERROR IN ORDER TO GENERATE TRACING OF CALLING SUBROUTINES.	JET0459
	X=-1.DO	JET0460
	Y=X+DSQRT(X)	JET0461
	IF(IFIN.LE.0) GO TO 100	JET0462
	STOP	JET0463
100	RETURN	JET0464
	END	JET0465
	SUBROUTINE MARCH	JET0466
C	SUBROUTINE NUMBER 5	JET0467
	IMPLICIT REAL*8(A-H,L-Z,*)	JET0468
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET0469
1	TETAF(101),BF(101),	JET0470
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),	JET0471
3	TETAN(101),BN(101),XTEMP(101)	JET0472
	COMMON/THICKY/XTH(1002),TH(1002)	JET0473
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,	JET0474
1	G16,G17,G18,G19,G20	JET0475
	COMMON /PAR/PA1,PA12,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,	JET0476
1	STAB,DELTA,PSI1,PSIF,ZETAL,SIGMA,FRACG,EPSIL,NUO,	JET0477
2	TETSYN,TETLIM,DDY,DYMAX	JET0478
	COMMON /STAG/RH00,NO,PO,TO,AO,MDOT1	JET0479
	COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,	JET0480
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD	JET0481
	COMMON /ROW/YF,YN,DXF,DXN	JET0482
	COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),	JET0483
1	RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),	JET0484
2	TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),	JET0485
3	CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),	JET0486
4	MCHARI(92)	JET0487
	COMMON /ICHARA/KCHARP,KCHARM,KCHARO	JET0488
C		JET0489
C	ADVANCE FLOW FIELD FROM YF TO YN	JET0490
	IM=KF	JET0491
	IP=KF	JET0492
	YN=YF+DY	JET0493
	KN=KF0	JET0494
C	SEMI-INVERSE INTEGRATION FOR FAN POINTS.	JET0495
	CALL SEMINV	JET0496
C	NEW GRID POINTS (JUST INVERSE MARCHING).	JET0497
	CALL GRIDN	JET0498
C	LOAD FLOW VARIABLES FROM SEMI-INVERSE INTEGRATION INTO VECTORS	JET0499
	CALL LOADC	JET0500
C	CHARACTERISTIC SCHEME INTEGRATION FOR INNER POINTS (INVERSE MARCH).	JET0501
	CALL INVMAR	JET0502
	RETURN	JET0503
	END	JET0504

FIN

MARCH

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SUBROUTINE INVMAR
C SUBROUTINE NUMBER 6
IMPLICIT REAL*8(A-H,L-Z,$)
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1      TETAF(101),BF(101),
2      XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3      TETAN(101),BN(101),XTEMP(101)
COMMON/THICKY/XTH(1002),TH(1002)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1      G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,
2      TETSYM,TETLIM,DDY,DYMAX
COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1      KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
COMMON /ROW/YF,YN,DXF,DXN
C
C INTEGRATION WITH INVERSE CHARACTERISTICS FOR NEW POINT(X4,Y4).
C OLD POINTS ARE (X1,Y1),(X2,Y2).
C X1 IS OBTAINED BY INVERSE C- FROM X4
C X2 IS OBTAINED BY INVERSE C+ FROM X4
C NOTE THAT X1 MAY BE NEGATIVE (E. G. WHEN X4=0).
KN1=ILEAD-1
IF(KN1.LE.0) CALL FIN(601)
DO 1000 I=1,KN1
I4=I
X4=XN(I)
Y4=YN
IF4=(IM+IP)/2
CALL INTERP(0,IF4,KF,X4,XF,RM4,RMF,RP4,RPF)
CALL RFUNC(RM4,RP4,M4,MU4,TETA4)
M14=M4
MU14=MU4
TETA14=TETA4
M24=M4
MU24=MU4
TETA24=TETA4
Y1=YF
Y2=YF
Y14=(Y1+Y4)/2.D0
Y24=(Y2+Y4)/2.D0
X1=1.D10
X2=1.D10
RM4=1.D10
RP4=1.D10
ITER=0
GO TO 2
C
C CORRECTOR
C
1 ITER=ITER+1
C AVERAGED PROPERTIES ON C-(14),C+(24) CHARACTERISTICS.
RM14=(RM1+RM4)/2.D0
RP14=(RP1+RP4)/2.D0
RM24=(RM2+RM4)/2.D0
RP24=(RP2+RP4)/2.D0
C M14,MU14,TETA14, M24,MU24,TETA24 AVERAGED ON C-,C+ CHARACTERISTICS.
CALL RFUNC(RM14,RP14,M14,MU14,TETA14)
CALL RFUNC(RM24,RP24,M24,MU24,TETA24)
2 CONTINUE
C NEW X1,X2
X10=X1
X20=X2
X1=X4-DY/DTAN(TETA14-MU14)
X2=X4-DY/DTAN(TETA24+MU24)
IF(X2.LT.0.) CALL FIN(670)
D14=DSQRT((X1-X4)**2+DY**2)
D24=DSQRT((X2-X4)**2+DY**2)
C INTERPOLATE OLD DISTRIBUTION FOR RM1,RP1, RM2,RP2 AT X1,X2.
CALL INTERP(0,IM,KF,X1,XF,RM1,RMF,RP1,RPF)
CALL INTERP(0,IP,KF,X2,XF,RM2,RMF,RP2,RPF)

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C NO NEED FOR RE-AVERAGING SINCE IT INTRODUCES ONLY HIGHER ORDER JET0577
C CHANGES INTO THE ITERATION SCHEME. JET0578
C INTEGRATE THE CHARACTERISTIC EQUATIONS FOR RM4,RP4 AT X4,Y4. JET0579
    RM40=RM4 JET0580
    RP40=RP4 JET0581
    RM4=RM1+DELTA*DS11*(TETA14)*D14/(M14*Y14) JET0582
    RP4=RP2+DELTA*DSIN(TETA24)*D24/(M24*Y24) JET0583
C CONVERGENCE TEST JET0584
    EPS=(DABS(X1-X10)+DABS(X2-X20))/DY+DABS(RM4-RM40)+DABS(RP4-RP40) JET0585
    IF(ITER.GT.ITER0) GO TO 10 JET0586
    IF(EPS.GT.EPSIL) GO TO 1 JET0587
    RMN(I)=RM4 JET0588
    RPN(I)=RP4 JET0589
    CALL RFUNC(RM4,RP4,MN(I),MUN(I),TETAN(I)) JET0590
1000 CONTINUE JET0591
    RETURN JET0592
10 CONTINUE JET0593
    PRINT 11,I4,KN,IF4,IM,IP,KF,ITER,ITER0,EPS,EPSIL,X1,X2,X4,M14,M24 JET0594
11 FORMAT(1X,'SUBR. INVMAR. I4,KN,IF4,IM,IP,KF,ITER,ITER0=',8I5/ JET0595
1 1X,'EPS,EPSIL,X1,X2,X4,M14,M24=',7D14.6/) JET0596
    CALL FIN(611) JET0597
    RETURN JET0598
    END JET0599

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SUBROUTINE SEMINV JET0600
C SUBROUTINE NUMBER 7 JET0601
    IMPLICIT REAL*8(A-H,L-Z,$) JET0602
    COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0603
1    TETAF(101),BF(101), JET0604
2    XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0605
3    TETAN(101),BN(101),XTEMP(101) JET0606
    COMMON/THICKY/XTH(1002),TH(1002) JET0607
    COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0608
1    G16,G17,G18,G19,G20 JET0609
    COMMON /PAR/PA1,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET0610
1    STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0, JET0611
2    TETSYN,TETLIM,DDY,DYMAX JET0612
    COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1 JET0613
    COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET0614
1    KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD JET0615
    COMMON /ROW/YF,YN,DXF,DXN JET0616
    COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET0617
1    RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET0618
2    TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET0619
3    CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET0620
4    MCHARI(92) JET0621
    COMMON /ICHARA/KCHARP,KCHARM,KCHARO JET0622
C COMPUTE NEW POINT (X4,Y4), BY PASSING A C+ CHARACTERISTIC JET0623
C THROUGH OLD POINT (X2,Y2). BOTH POINTS ARE ON CHARACTERISTIC LINE JET0624
C NUMBER KC. JET0625
    IM=1 JET0626
    DO 100 KC=1,KCHARO JET0627
    IF(CSIGNN(KC).EQ.0.) GO TO 100 JET0628
C PREDICTOR JET0629
C JET0630
C JET0631
    Y1=YF JET0632
    Y2=YF JET0633
    Y4=YN JET0634
    Y14=(Y1+Y4)/2.DO JET0635
    Y24=(Y2+Y4)/2.DO JET0636
    X2=XCHARF(KC) JET0637
    RM2=RMCARF(KC) JET0638
    RP2=RPCARF(KC) JET0639
    M2=MCHARF(KC) JET0640
    MU2=MUCARF(KC) JET0641
    TETA2=TCHARF(KC) JET0642
    M14=M2 JET0643
    MU14=MU2 JET0644
    TETA14=TETA2 JET0645
    M24=M2 JET0646
    MU24=MU2 JET0647
    MU24=MU2 JET0648

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      TETA24=TETA2
      X4=1.D10
      X1=1.D10
      RM4=1.D10
      RP4=1.D10
      ITER=0
      GO TO 2
C
C CORRECTOR
C
1  ITER=ITER+1
C AVERAGED PROPERTIES ON C-(14),C+(24) CHARACTERISTICS.
      RM14=(RM1+RM4)/2.D0
      RP14=(RP1+RP4)/2.D0
      RM24=(RM2+RM4)/2.D0
      RP24=(RP2+RP4)/2.D0
C M14,MU14,TETA14, M24,MU24,TETA24 AVERAGED ON C-,C+ CHARACTERISTICS.
      CALL RFUNC(RM14,RP14,M14,MU14,TETA14)
      CALL RFUNC(RM24,RP24,M24,MU24,TETA24)
2  CONTINUE
C NEW X4,X1
      X40=X4
      X10=X1
      X4=X2+DY/DTAN(TETA24+CSIGNF(KC)*MU24)
      X1=X4-DY/DTAN(TETA14-CSIGNF(KC)*MU14)
      D14=DSQRT((X1-X4)**2+DY**2)
      D24=DSQRT((X2-X4)**2+DY**2)
C INTERPOLATE OLD DISTRIBUTION FOR RM1,RP1, AT X1.
      CALL INTERP(0,IM,KF,X1,XF,RM1,RMF,RP1,RPF)
      IF(J.GT.1) GO TO 22
      IF(CSIGNF(KC).LT.0.) GO TO 22
      RP1=RP2
22  CONTINUE
C NO NEED FOR RE-AVERAGING SINCE IT INTRODUCES ONLY HIGHER ORDER
C CHANGES INTO THE ITERATION SCHEME.
C INTEGRATE THE CHARACTERISTIC EQUATIONS FOR RM4,RP4 AT X4,Y4.
      RM40=RM4
      RP40=RP4
      IF(CSIGNF(KC).LT.0.) GO TO 21
      RM4=RM1+DELTA*DSIN(TETA14)*D14/(M14*Y14)
      RP4=RP2+DELTA*DSIN(TETA24)*D24/(M24*Y24)
      GO TO 20
21  CONTINUE
      RM4=RM2+DELTA*DSIN(TETA24)*D24/(M24*Y24)
      RP4=RP1+DELTA*DSIN(TETA14)*D14/(M14*Y14)
20  CONTINUE
C CONVERGENCE TEST
      EPS=(DABS(X4-X40)+DABS(X1-X10))/DY+DABS(RM4-RM40)+DABS(RP4-RP40)
      IF(ITER.GT.ITER0) GO TO 10
      IF(EPS.GT.EPSIL) GO TO 1
      CSIGNN(KC)=CSIGNF(KC)
      IF(X4.GT.0.) GO TO 30
      RMSAVE=RM4
      RM4=RP4+TETSYN
      RP4=RM4-TETSYN
      CSIGNN(KC)=-1.D0
30  CONTINUE
      RMCARN(KC)=RM4
      RPCARN(KC)=RP4
      CALL RFUNC(RM4,RP4,M4,MU4,TETA4)
      TCHARN(KC)=TETA4
      XCHARN(KC)=DABS(X4)
      YCHARN(KC)=Y4
      MUCARN(KC)=MU4
      MCHARN(KC)=M4
100 CONTINUE
      RETURN
10  CONTINUE
      PRINT 11,KC,KCHAR0,IM,KF,ITER,ITER0,EPS,EPSIL,X1,X2,X4,M14,M24
11  FORMAT(1X,'SUBR. SEMINV. KC,KCHAR0,IM,KF,ITER,ITER0=',6I5/
1  1X,'EPS,EPSIL,X1,X2,X4,M14,M24=',7D14.6/)
      CALL FIN(711)

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JET0649
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 JET0720

	RETURN END	RFUNC	JET0721 JET0722
	SUBROUTINE RFUNC(RM,RP,M,MU,TETA)		JET0723
C	SUBROUTINE NUMBER 8		JET0724
	IMPLICIT REAL*8(A-H,L-Z,\$)		JET0725
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),		JET0726
1	TETAF(101),BF(101),		JET0727
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),		JET0728
3	TETAN(101),BN(101),XTEMP(101)		JET0729
	COMMON/THICKY/XTH(1002),TH(1002)		JET0730
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,		JET0731
1	G16,G17,G18,G19,G20		JET0732
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,		JET0733
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,		JET0734
2	TETSYM,TETLIM,DDY,DYMAX		JET0735
	COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1		JET0736
	COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,		JET0737
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD		JET0738
	COMMON /ROW/YF,YN,DXF,DXN		JET0739
C	COMPUTE M,MU,TETA AT A POINT, AS FUNCTION OF RIEMANN INVAR. RM,RP.		JET0740
C	TETA=(RM-RP)/2.D0+TETLIM		JET0741
	NU =(RM+RP)/2.D0		JET0742
C	NU=NU0-(G5*ARCTAN(G5*Q)-ARCTAN(Q)), WHERE Q=(M**2-1)**(-1/2)		JET0743
C	FIND Q(NU), AND HENCE M(NU), THROUGH NEWTON RAPHSON ITERATIONS.		JET0744
	Q=-((NU-NU0)/(G4-1.D0))		JET0745
	IF(Q.LE.0.) CALL FIN(801)		JET0746
	ITER=0		JET0747
1	ITER=ITER+1		JET0748
	QF=Q		JET0749
	DNUDT=-((G4-1.D0)/((1.D0+G4*Q**2)*(1.D0+Q**2)))		JET0750
	DNU=NU-(NU0-(G5*DATAN(G5*Q)-DATAN(Q)))		JET0751
	Q=Q+DNU/DNUDT		JET0752
	IF(Q.LE.0.) CALL FIN(811)		JET0753
	EPS=DABS(Q-QF)/Q		JET0754
	IF(ITER.GT.ITER0) GO TO 10		JET0755
	IF(EPS.GT.EPSIL*1.D-3) GO TO 1		JET0756
	M=DSQRT(1.D0+1.D0/Q**2)		JET0757
	MU=DARSIN(1.D0/M)		JET0758
	RETURN		JET0759
10	CONTINUE		JET0760
	CALL FIN(810)		JET0761
	RETURN		JET0762
	END	INTERP	JET0763
	SUBROUTINE INTERP(JNEW,I,KGRID,X,XVEC,RM,RMVEC,RP,RPVEC)		JET0764
C	SUBROUTINE NUMBER 9		JET0765
	IMPLICIT REAL*8(A-H,L-Z,\$)		JET0766
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),		JET0767
1	TETAF(101),BF(101),		JET0768
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),		JET0769
3	TETAN(101),BN(101),XTEMP(101)		JET0770
	COMMON/THICKY/XTH(1002),TH(1002)		JET0771
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,		JET0772
1	G16,G17,G18,G19,G20		JET0773
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,		JET0774
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,		JET0775
2	TETSYM,TETLIM,DDY,DYMAX		JET0776
	COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1		JET0777
	COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,		JET0778
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD		JET0779
	COMMON /ROW/YF,YN,DXF,DXN		JET0780
	DIMENSION XVEC(1),RMVEC(1),RPVEC(1)		JET0781
C	FIND I SUCH THAT XVEC(I).LE.X.AND.XVEC(I+1).GE.X		JET0782
C	FIND RM,RP BY LINEAR INTERPOLATION.		JET0783
C	NOTE THAT X MAY BE NEGATIVE.		JET0784
	IF(DABS(X).LE.XVEC(KGRID)) GO TO 901		JET0785
	PRINT 900,X,KGRID,XVEC(KGRID)		JET0786
	FORMAT(/1X,D15.7,I10,4X,D15.7/)		JET0787
	CALL FIN(900)	JET0789	JET0788
901	CONTINUE		JET0790
	KG2=2*KGRID		JET0791
			JET0792

	I0=MIN0(I,KGRID-2)	JET0793
	ICOUNT=0	JET0794
1	I=I0	JET0795
	SIGN1=1.D0	JET0796
	IF(I.GE.1) GO TO 10	JET0797
	SIGN1=-1.D0	JET0798
	I=-I+2	JET0799
10	CONTINUE	JET0800
	IF(I.GT.KGRID) CALL FIN(901)	JET0801
	XX1=SIGN1*XVEC(I)	JET0802
	I1=I	JET0803
	IF(XX1.LE.X) GO TO 11	JET0804
	I0=I0-1	JET0805
	ICOUNT=ICOUNT+1	JET0806
	IF(ICOUNT.GT.KG2) CALL FIN(911)	JET0807
	GO TO 1	JET0808
11	CONTINUE	JET0809
	I=I0+1	JET0810
	SIGN2=1.D0	JET0811
	IF(I.GE.1) GO TO 12	JET0812
	SIGN2=-1.D0	JET0813
	I=-I+2	JET0814
12	CONTINUE	JET0815
	IF(I.GT.KGRID) CALL FIN(912)	JET0816
	XX2=SIGN2*XVEC(I)	JET0817
	I2=I	JET0818
	IF(XX2.GE.X) GO TO 13	JET0819
	I0=I0+1	JET0820
	ICOUNT=ICOUNT+1	JET0821
	IF(ICOUNT.GT.KG2) CALL FIN(913)	JET0822
	GO TO 1	JET0823
13	CONTINUE	JET0824
	F1=(XX2-X)/(XX2-XX1)	JET0825
	F2=1.D0-F1	JET0826
	IF(F1.LT.0.) CALL FIN(991)	JET0827
	IF(F2.LT.0.) CALL FIN(992)	JET0828
	RM1=RMF(I1)	JET0829
	RP1=RPF(I1)	JET0830
	RM2=RMF(I2)	JET0831
	RP2=RPF(I2)	JET0832
	IF(SIGN1.LT.0.) RM1=RPF(I1)+TETSYM	JET0833
	IF(SIGN1.LT.0.) RP1=RMF(I1)-TETSYM	JET0834
	IF(SIGN2.LT.0.) RM2=RPF(I2)+TETSYM	JET0835
	IF(SIGN2.LT.0.) RP2=RMF(I2)-TETSYM	JET0836
	RM=F1*RM1+F2*RM2	JET0837
	RP=F1*RP1+F2*RP2	JET0838
	RETURN	JET0839
	END	JET0840
	INTERX	
	SUBROUTINE INTERX(JNEW,I1,VAR0,VAR,KGRID,X0,XVEC)	JET0841
C	SUBROUTINE NUMBER 10	JET0842
	IMPLICIT REAL*8(A-H,L-Z,*)	JET0843
	COMMON /VECS/ XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET0844
1	TETAF(101),BF(101),	JET0845
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),	JET0846
3	TETAN(101),BN(101),XTEMP(101)	JET0847
	COMMON/THICKY/XTH(1002),TH(1002)	JET0848
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,	JET0849
1	G16,G17,G18,G19,G20	JET0850
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,	JET0851
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,	JET0852
2	TETSYM,TETLIM,DDY,DYMAX	JET0853
	COMMON /STAG/RH00,NO,P0,TO,A0,MDOT1	JET0854
	COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,	JET0855
1	KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD	JET0856
	COMMON /ROW/YF,YN,DXF,DXN	JET0857
	DIMENSION VAR(1),XVEC(1)	JET0858
C	FIND X0 AND I1 SUCH THAT XVEC(I1)<X0<XVEC(I1+1), AND X0 CORRESPONDS	JET0859
C	TO THE LOCATION AT WHICH VAR0 IS A LINEAR INTERPOLATION OF VAR(I).	JET0860
	X0=1.D23	JET0861
	IFIRST=I1	JET0862
	IF(I1.GT.0) GO TO 10	JET0863
	IFIRST=KGRID-IABS(I1)+2	JET0864

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10 CONTINUE JET0865
DO 1 II=IFIRST,KGRID JET0866
I=II JET0867
IF(I1.GT.0) GO TO 11 JET0868
I=KGRID-II+2 JET0869
11 CONTINUE JET0870
IF(I.LE.0) CALL FIN(1001) JET0871
IF(I.GT.KGRID) CALL FIN(1002) JET0872
IF(I.EQ.1) GO TO 1 JET0873
IF((VAR(I)-VAR0)*(VAR(I-1)-VAR0).GT.0.) GO TO 1 JET0874
IF(VAR(I).EQ.VAR(I-1)) GO TO 1 JET0875
F1=(VAR(I)-VAR0)/(VAR(I)-VAR(I-1)) JET0876
F2=1.D0-F1 JET0877
IF(F1.LT.0.) CALL FIN(1011) JET0878
IF(F2.LT.0.) CALL FIN(1012) JET0879
X0=F1*XVEC(I-1)+F2*XVEC(I) JET0880
I1=I-1 JET0881
GO TO 2 JET0882
1 CONTINUE JET0883
2 CONTINUE JET0884
RETURN JET0885
END JET0886

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BREAK

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SUBROUTINE BREAK JET0887
C SUBROUTINE NUMBER 11 JET0888
IMPLICIT REAL*8(A-H,L-Z,$) JET0889
REAL MB,MX,MY JET0890
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0891
1 TETAF(101),BF(101), JET0892
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0893
3 TETAN(101),BN(101),XTEMP(101) JET0894
COMMON/THICKY/XTH(1002),TH(1002) JET0895
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0896
1 G16,G17,G18,G19,G20 JET0897
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET0898
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0, JET0899
2 TETSYM,TETLIM,DDY,DYMAX JET0900
COMMON /STAG/RH00,N0,P0,T0,A0,MDOT1 JET0901
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET0902
1 KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET0903
COMMON /ROW/YF,YN,DXF,DXN JET0904
C JET0905
C COMPUTE THE BREAKDOWN PARAMETER AT (I-1/2,K-1/2). STORE IN BN(I). JET0906
YB=0.5D0*(YF+YN) JET0907
DYY=DY JET0908
IM=2 JET0909
DO 1 I=2,KN JET0910
X1=XN(I-1) JET0911
X2=XN(I) JET0912
DXX=X2-X1 JET0913
IF(X2.GT.XF(KF)) GO TO 2 JET0914
CALL INTERP(0,IM,KF,X1,XF,RM1,RMF,RP1,RPF) JET0915
CALL INTERP(0,IM,KF,X2,XF,RM2,RMF,RP2,RPF) JET0916
CALL RFUNC(RM1,RP1,M1,MU1,TETA1) JET0917
CALL RFUNC(RM2,RP2,M2,MU2,TETA2) JET0918
MX=0.5D0*((MN(I)-MN(I-1))+(M2-M1))/DXX JET0919
MY=0.5D0*((MN(I)-M2)+(MN(I-1)-M1))/DYY JET0920
MB=0.25D0*(MN(I-1)+MN(I)+M1+M2) JET0921
TETAB=0.25D0*(TETAN(I-1)+TETAN(I)+TETA1+TETA2) JET0922
GOREM=MB**2*(1.D0+G1*MB**2)**(G6-1.D0) JET0923
GRAD=MX*DCOS(TETAB)+MY*DSIN(TETAB) JET0924
B=G20*GOREM*GRAD JET0925
GO TO 3 JET0926
2 B=1.D22 JET0927
3 BN(I)=B JET0928
1 CONTINUE JET0929
BN(1)=BN(2) JET0930
RETURN JET0931
END JET0932

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OPACY

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SUBROUTINE OPACY JET0933
C SUBROUTINE NUMBER 12 JET0934
IMPLICIT REAL*8(A-H,L-Z,$) JET0935
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0936

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1      TETAF(101),BF(101), JET0937
2      XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0938
3      TETAN(101),BN(101),XTEMP(101) JET0939
COMMON/THICKY/XTH(1002),TH(1002) JET0940
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0941
1      G16,G17,G18,G19,G20 JET0942
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET0943
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET0944
2      TETSYN,TETLIM,DDY,DYMAX JET0945
COMMON /STAG/RH00,N0,P0,T0,A0,MDOT1 JET0946
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET0947
1      KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET0948
COMMON /ROW/YF,YN,DXF,DXN JET0949
C JET0950
C COMPUTE THE MOLECULAR THICKNESS AT END POINTS OF EACH ROW. JET0951
IM=2 JET0952
XTH(J)=XF(KF) JET0953
TH(J)=0. JET0954
DTH0=N0*SIGMA*DY JET0955
IF(J.EQ.1) GO TO 11 JET0956
J1=J-1 JET0957
DO 1 JJ=1,J1 JET0958
XX1=XTH(JJ) JET0959
CALL INTERP(0,IM,KF,XX1,XF,RM1,RMF,RP1,RPF) JET0960
CALL RFUNC(RM1,RP1,M1,MU1,TETA1) JET0961
GOREM=1.D0+G1*M1**2 JET0962
DTH=DTH0/GOREM**G6 JET0963
TH(JJ)=TH(JJ)+DTH JET0964
1 CONTINUE JET0965
11 CONTINUE JET0966
RETURN JET0967
END JET0968
SUBROUTINE PLUMES JET0969
C SUBROUTINE NUMBER 13 JET0970
IMPLICIT REAL*8(A-H,L-Z,$) JET0971
REAL*4 XPL,YPL JET0972
COMMON /PLUME/XPL(1002,10),YPL(1002) JET0973
COMMON /IPLUME/KPL,ITYPL(10) JET0974
DIMENSION VPL(92) JET0975
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET0976
1 TETAF(101),BF(101), JET0977
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET0978
3 TETAN(101),BN(101),XTEMP(101) JET0979
COMMON/THICKY/XTH(1002),TH(1002) JET0980
REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF JET0981
COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20) JET0982
1 XIAPP(101,20),XIF(101,20) JET0983
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET0984
1 G16,G17,G18,G19,G20 JET0985
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET0986
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET0987
2 TETSYN,TETLIM,DDY,DYMAX JET0988
COMMON /STAG/RH00,N0,P0,T0,A0,MDOT1 JET0989
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET0990
1 KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET0991
COMMON /ROW/YF,YN,DXF,DXN JET0992
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET0993
1 RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET0994
2 TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET0995
3 CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET0996
4 MCHARI(92) JET0997
COMMON /ICHARA/KCHARP,KCHARM,KCHARO JET0998
C COMPUTE SPECIAL POINTS AT Y=YN, AND STORE THEM AS JET0999
C (XPL(J,IPL),YPL(J)=YN). JET1000
C J IS THE MARCHING INDEX OF YN. JET1001
C IPL=1,2,...,KPL IS THE "PLUME" INDEX. PRESENTLY KPL.LE.5 JET1002
C VPL(IPL) IS A VALUE DEFINING THE "PLUME" CURVE. JET1003
C ITYPL(IPL) IS THE TYPE OF CURVE. IT DEFINES CURVES AS FOLLOWS: JET1004
C ITYPL(IPL)=0 DO NOTHING JET1005
C ITYPL(IPL)=1 REAL PLUME. IT IS THE BREAKDOWN SURFACE, DEFINED JET1006
C BY A CONSTANT VALUE OF THE BREAKDOWN PARAMETER B. JET1007
C SET VPL(IPL)=B. JET1008

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PLUMES

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C  ITYPL(IPL)=2  CONSTANT MACH-NUMBER LINE.  VPL(IPL)=M.          JET1009
C  ITYPL(IPL)=3  A SINGLE STREAMLINE.  VPL(IPL) IS SET TO THE EXIT JET1010
C  X-COORDINATE OF THAT STREAMLINE.          JET1011
C  ITYPL(IPL)=4  A SINGLE C+ CHARACTERISTIC LINE STARTING AT THE CORNER. JET1012
C  VPL(IPL) IS SET TO THE INDEX KC OF THAT CHARACTERISTIC JET1013
C  LINE.          JET1014
C  ITYPL(IPL)=5  A CONSTANT LATERAL (X) OPACITY LINE.  VPL(IPL) IS SET JET1015
C  TO THE VALUE OF THE (CONSTANT) OPACITY.    JET1016
C  JET1017
C  DEFINE ITYPL(IPL) AND VPL(IPL)             JET1018
C  KPL=10                                     JET1019
C  IF(KPL.GT.10) CALL FIN(1301)               JET1020
C  DO 2000 IPL=1,KPL                          JET1021
C  GO TO (2001,2002,2003,2004,2005,2006,2007,2008,2009,2010),IPL JET1022
2001 ITYPL(IPL)=4                             JET1023
C  VPL(IPL)=1                                JET1024
C  GO TO 2000                                JET1025
2002 ITYPL(IPL)=4                             JET1026
C  VPL(IPL)=KCHARP                           JET1027
C  GO TO 2000                                JET1028
2003 ITYPL(IPL)=4                             JET1029
C  VPL(IPL)=19                               JET1030
C  GO TO 2000                                JET1031
2004 ITYPL(IPL)=4                             JET1032
C  VPL(IPL)=31                               JET1033
C  GO TO 2000                                JET1034
2005 ITYPL(IPL)=4                             JET1035
C  VPL(IPL)=47                               JET1036
C  GO TO 2000                                JET1037
2006 ITYPL(IPL)=4                             JET1038
C  VPL(IPL)=55                               JET1039
C  GO TO 2000                                JET1040
2007 ITYPL(IPL)=1                             JET1041
C  VPL(IPL)=0.02D0                           JET1042
C  GO TO 2000                                JET1043
2008 ITYPL(IPL)=1                             JET1044
C  VPL(IPL)=0.03D0                           JET1045
C  GO TO 2000                                JET1046
2009 ITYPL(IPL)=1                             JET1047
C  VPL(IPL)=0.05D0                           JET1048
C  GO TO 2000                                JET1049
2010 ITYPL(IPL)=1                             JET1050
C  VPL(IPL)=0.08D0                           JET1051
C  GO TO 2000                                JET1052
2000 CONTINUE                                JET1053
C  COMPUTE "PLUME" POINTS AT Y=YN             JET1054
C  DO 1000 IPL=1,KPL                          JET1055
C  ITYP=ITYPL(IPL)                            JET1056
C  IF(ITYP.EQ.0) GO TO 1000                   JET1057
C  GO TO (1,2,3,4,5), ITYP                   JET1058
1  CONTINUE                                JET1059
C  BREAKDOWN SURFACE PLUME.                   JET1060
C  NOTE THAT DUE TO DIFFERENCE-CENTERING OF GRADIENTS, THE ACCURATE JET1061
C  Y-COORDINATE IS 0.5*(YF+YN), RATHER THAN YN. IT CAN BE ADJUSTED JET1062
C  IN THE PLOTTING CODE.                     JET1063
C  BO=VPL(IPL)                                JET1064
C  XTEMP(1)=XN(1)                             JET1065
C  DO 11 I=2,KN                               JET1066
C  XTEMP(I)=0.5D0*(XN(I)+XN(I-1))           JET1067
11  CONTINUE                                JET1068
C  I=2                                         JET1069
C  CALL INTERX(1,I,BO,BN,KN,XBO,XTEMP)       JET1070
C  XPL(J,IPL)=XBO                             JET1071
C  GO TO 1001                                JET1072
2  CONTINUE                                JET1073
C  FIND BY INTERPOLATION THE X-COORDINATE WHERE M=MPL. JET1074
C  IF(J.GT.1) GO TO 200                       JET1075
C  XPL(J,IPL)=XC                             JET1076
C  GO TO 1001                                JET1077
200  CONTINUE                                JET1078
C  MPL=VPL(IPL)                              JET1079
C  I=-KN                                     JET1080
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CALL INTERX(1,I,MPL,MN,KN,XM0,XN)	JET1081
XPL(J,IPL)=XM0	JET1082
GO TO 1001	JET1083
3 CONTINUE	JET1084
C STREAMLINE INTERPOLATION.	JET1085
IF(J.GT.1) GO TO 300	JET1086
XPL(J,IPL)=VPL(IPL)	JET1087
GO TO 1001	JET1088
300 CONTINUE	JET1089
XSF=XPL(J-1,IPL)	JET1090
ISF=2	JET1091
ISN=2	JET1092
CALL INTERP(0,ISF,KF,XSF,XF,RMSF,RMF,RPSF,RPF)	JET1093
CALL RFUNC(RMSF,RPSF,MSF,MUSF,TETASF)	JET1094
XSN=XSF+DY*DTAN(PIA2-TETASF)	JET1095
ITER=1	JET1096
301 ITER=ITER+1	JET1097
CALL INTERP(1,ISN,KN,XSN,XN,RMSN,RMN,RPSN,RPN)	JET1098
CALL RFUNC(RMSN,RPSN,MSN,MUSN,TETASN)	JET1099
TETAASV=0.5D0*(TETASF+TETASN)	JET1100
XSN=XSF+DY*DTAN(PIA2-TETAASV)	JET1101
IF(ITER.LT.ITER0+2) GO TO 301	JET1102
XPL(J,IPL)=XSN	JET1103
GO TO 1001	JET1104
4 CONTINUE	JET1105
C CHARACTERISTIC LINE.	JET1106
KC=IDINT(VPL(IPL)+1.D-5)	JET1107
IF(J.GT.1) GO TO 41	JET1108
XPL(J,IPL)=XCHARF(KC)	JET1109
GO TO 1001	JET1110
41 CONTINUE	JET1111
XPL(J,IPL)=XCHARN(KC)	JET1112
IF(CSIGNN(KC).EQ.0.) XPL(J,IPL)=1.E33	JET1113
GO TO 1001	JET1114
5 CONTINUE	JET1115
C CONSTANT LATERAL (X) OPACITY	JET1116
CALL OPACX	JET1117
XIC=VPL(IPL)	JET1118
DO 51 II=2,KF	JET1119
I1=KF-II+1	JET1120
I2=I1+1	JET1121
XI1=XI(I1,JXI)	JET1122
XI2=XI(I2,JXI)	JET1123
IF((XIC-XI1)*(XIC-XI2).GT.0.) GO TO 51	JET1124
F2=(XI2-XIC)/(XI2-XI1)	JET1125
F1=1.D0-F2	JET1126
IF(F1.LT.0.) CALL FIN(1351)	JET1127
IF(F2.LT.0.) CALL FIN(1352)	JET1128
XIFC=F2*XF(I1)+F1*XF(I2)	JET1129
GO TO 52	JET1130
51 CONTINUE	JET1131
XIFC=1.D30	JET1132
52 CONTINUE	JET1133
XPL(J,IPL)=XIFC	JET1134
GO TO 1001	JET1135
1001 CONTINUE	JET1136
IF(J.GT.1) GO TO 1002	JET1137
YPL(J)=YC	JET1138
GO TO 1000	JET1139
1002 CONTINUE	JET1140
YPL(J)=YN	JET1141
1000 CONTINUE	JET1142
RETURN	JET1143
END	JET1144
GRIDN	
SUBROUTINE GRIDN	JET1145
C SUBROUTINE NUMBER 14	JET1146
IMPLICIT REAL*8(A-H,L-Z,*)	JET1147
REAL*4 XPL,YPL	JET1148
COMMON /PLUME/XPL(1002,10),YPL(1002)	JET1149
COMMON /IPLUME/KPL,ITYPL(10)	JET1150
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET1151
1 TETAF(101),BF(101),	JET1152

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2          XN(101),RMN(101),RPN(101),MN(101),MUN(101),      JET1153
3          TETAN(101),BN(101),XTEMP(101)                    JET1154
COMMON/THICKY/XTH(1002),TH(1002)                             JET1155
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1156
1          G16,G17,G18,G19,G20                                JET1157
COMMON /PAR/PA1,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1158
1          STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,   JET1159
2          TETSYM,TETLIM,DDY,DYMAX                           JET1160
COMMON /STAG/RH00,NO,P0,T0,A0,MDO1                          JET1161
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,                  JET1162
1          KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD        JET1163
COMMON /ROW/YF,YN,DXF,DXN                                    JET1164
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),   JET1165
1          RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),      JET1166
2          TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),      JET1167
3          CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),      JET1168
4          MCHARI(92)                                         JET1169
COMMON /ICHARA/KCHARP,KCHARM,KCHARO                          JET1170
C  DIVIDE LINE Y=YN INTO KN-1 INTERVALS.                     JET1171
C  THE X-GRID IS NON-UNIFORMLY DEFINED AS FOLLOWS:          JET1172
C  (1) (XCHARN(I),YCHARN(I)), (XCHARF(I),YCHARF(I)), I=1,2,...,KCHARP, JET1173
C      DENOTE NEW AND OLD (FORMER) CHARACTERISTIC (C+) POINTS. LET I=1 JET1174
C      AND I=KCHARP CORRESPOND TO THE LEADING AND BOUNDARY JET1175
C      CHARACTERISTICS (C+).                                  JET1176
C  (2) THE GRID CONSISTS OF TWO SEGMENTS. THE SO-CALLED FLAT SEGMENT JET1177
C      IS BETWEEN X=0 AND X=XLEAD=XCHARN(KCLEAD). THE SECOND IS THE JET1178
C      FAN SEGMENT. IT IS FROM XLEAD TO XBOUND=XCHARN(KCHARP). JET1179
C  (3) THE FAN SEGMENT IS INITIALLY DIVIDED INTO FRACG*(KF0-1) INTERVALS JET1180
C      DEFINED BY THE FAMILY OF C+ CHARACTERISTIC LINES MCHARI(1) TO JET1181
C      MCHARI(KCHARP).                                       JET1182
C  (4) THE FLAT SEGMENT IS DIVIDED INTO (1-FRACG)*(KF0-1) EQUAL JET1183
C      INTERVALS, AS LONG AS THEY ARE NOT SMALLER THAN THE AVERAGE JET1184
C      FAN INTERVAL. WHEN THEY ARE, THEIR NUMBER IS REDUCED, BUT NOT JET1185
C      BELOW THREE.                                          JET1186
C  (5) KCLEAD IS INITIALLY 1. IT IS UPDATED SO THAT THE FLAT SEGMENT JET1187
C      IS AT LEAST TWICE THE AVERAGE FAN INTERVAL.          JET1188
      ILEADF=ILEAD                                           JET1189
      KCLEAD=0                                               JET1190
      DO 1 KC=1,KCHARP                                       JET1191
      IF(CSIGNN(KC).LT.0.) GO TO 1                            JET1192
      KCLEAD=KC                                              JET1193
      KFAN=KCHARP-KCLEAD                                     JET1194
      XLEAD=XCHARN(KCLEAD)                                   JET1195
      XBOUND=XCHARN(KCHARP)                                  JET1196
      DX1=(XBOUND-XLEAD)/DFLOAT(KFAN)                       JET1197
      IF(XLEAD/DX1.GT.2.D0) GO TO 11                         JET1198
1      CONTINUE                                             JET1199
11     CONTINUE                                             JET1200
      IF(KCLEAD.EQ. 0) CALL FIN(1401)                        JET1201
      IF(KCLEAD.EQ.KCHARP) CALL FIN(1402)                   JET1202
      ILEAD=IDINT(XLEAD/DX1)+2                               JET1203
      IF(ILEAD+KFAN.GT.KF0) ILEAD=KF0-KFAN                  JET1204
      ILEAD1=ILEAD-1                                         JET1205
      KN=ILEAD+KFAN                                          JET1206
      IF(KN.GT.KF0) CALL FIN(1411)                           JET1207
      DX=XLEAD/DFLOAT(ILEAD1)                                JET1208
      XN(1)=0.                                               JET1209
      DO 2 I=1,ILEAD1                                       JET1210
      XN(I)=XN(1)+DX*DFLOAT(I-1)                             JET1211
2      CONTINUE                                             JET1212
      DO 3 I=ILEAD,KN                                       JET1213
      XN(I)=XCHARN(KCLEAD+I-ILEAD)                           JET1214
3      CONTINUE                                             JET1215
      RETURN                                                 JET1216
      END                                                    JET1217
SUBROUTINE YSTEP                                           JET1218
C  SUBROUTINE NUMBER 15                                     JET1219
      IMPLICIT REAL*8(A-H,L-Z,*)                             JET1220
      REAL*4 XPL,YPL                                         JET1221
      COMMON /PLUME/XPL(1002,10),YPL(1002)                  JET1222
      COMMON /IPLUME/KPL,ITYPL(10)                           JET1223
      COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET1224

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YSTEP

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1      TETAF(101),BF(101), JET1225
2      XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET1226
3      TETAN(101),BN(101),XTEMP(101) JET1227
COMMON/THICKY/XTH(1002),TH(1002) JET1228
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1229
1      G16,G17,G18,G19,G20 JET1230
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1231
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0, JET1232
2      TETSYM,TETLIM,DDY,DYMAX JET1233
COMMON /STAG/RH00,NO,PO,TO,A0,MDOT1 JET1234
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET1235
1      KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET1236
COMMON /ROW/YF,YN,DXF,DXN JET1237
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET1238
1      RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET1239
2      TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET1240
3      CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET1241
4      MCHARI(92) JET1242
COMMON /ICHARA/KCHARP,KCHARM,KCHARO JET1243
C COMPUTE NEXT Y-STEP. JET1244
C DYNEXT IS DEFINED AS THE MINIMAL "TRIANGULATION" Y-STEP DYT, OBTAINED JET1245
C BY FORWARD INTERSECTION OF C-,C+ CHARACTERISTICS FROM ADJACENT GRID JET1246
C POINTS X1,X2. JET1247
DYMIN=1.D40 JET1248
DO 1 I=3,KF JET1249
X1=XF(I-1) JET1250
X2=XF(I) JET1251
DX=X2-X1 JET1252
TP1=DTAN(TETAF(I-1)-MUF(I-1)) JET1253
TP2=DTAN(TETAF(I)+MUF(I)) JET1254
F1=-TP2/(TP1-TP2) JET1255
IF(F1.LE.0.) PRINT 555,I,X1,X2,DX,TP1,TP2,F1 JET1256
555 FORMAT(/1X,'I,X1,X2,DX,TP1,TP2,F1=',I5,6D14.6/) JET1257
IF(F1.LT.0.) CALL FIN(1501) JET1258
DYT=F1*DX*TP1 JET1259
IF(DYT.LE.0.) CALL FIN(1502) JET1260
DYMIN=DMIN1(DYMIN,STAB*DYT) JET1261
1 CONTINUE JET1262
DYNEXT=DYMIN JET1263
RETURN JET1264
END JET1265
MOVE
SUBROUTINE MOVE JET1266
C SUBROUTINE NUMBER 16 JET1267
IMPLICIT REAL*8(A-H,L-Z,*) JET1268
REAL*4 XPL,YPL JET1269
COMMON /PLUME/XPL(1002,10),YPL(1002) JET1270
COMMON /IPLUME/KPL,ITYPL(10) JET1271
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET1272
1      TETAF(101),BF(101), JET1273
2      XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET1274
3      TETAN(101),BN(101),XTEMP(101) JET1275
COMMON/THICKY/XTH(1002),TH(1002) JET1276
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1277
1      G16,G17,G18,G19,G20 JET1278
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1279
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0, JET1280
2      TETSYM,TETLIM,DDY,DYMAX JET1281
COMMON /STAG/RH00,NO,PO,TO,A0,MDOT1 JET1282
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET1283
1      KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET1284
COMMON /ROW/YF,YN,DXF,DXN JET1285
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET1286
1      RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET1287
2      TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET1288
3      CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET1289
4      MCHARI(92) JET1290
COMMON /ICHARA/KCHARP,KCHARM,KCHARO JET1291
C STORE NEW LINE (N) IN OLD LINE (F). JET1292
KF=KN JET1293
KF2=2*KF JET1294
YF=YN JET1295
DO 1 I=1,KN JET1296

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	XF(I)=XN(I)	JET1297
	RMF(I)=RMN(I)	JET1298
	RPF(I)=RPN(I)	JET1299
	MF(I)=MN(I)	JET1300
	MUF(I)=MUN(I)	JET1301
	TETAF(I)=TETAN(I)	JET1302
	BF(I)=BN(I)	JET1303
1	CONTINUE	JET1304
	DO 2 KC=1,KCHAR0	JET1305
	IF(CSIGNN(KC).EQ.0.) GO TO 2	JET1306
	XCHARF(KC)=XCHARN(KC)	JET1307
	YCHARF(KC)=YCHARN(KC)	JET1308
	RMCHARF(KC)=RMCARN(KC)	JET1309
	RPCARF(KC)=RPCARN(KC)	JET1310
	TCHARF(KC)=TCHARN(KC)	JET1311
	MUCARF(KC)=MUCARN(KC)	JET1312
	MCHARF(KC)=MCHARN(KC)	JET1313
	CSIGNF(KC)=CSIGNN(KC)	JET1314
2	CONTINUE	JET1315
	RETURN	JET1316
	END	JET1317
	OPACX	
	SUBROUTINE OPACX	JET1318
C	SUBROUTINE NUMBER 17	JET1319
	IMPLICIT REAL*8(A-H,L-Z,*)	JET1320
	REAL*4 XPL,YPL	JET1321
	COMMON /PLUME/XPL(1002,10),YPL(1002)	JET1322
	COMMON /IPLUME/KPL,ITYPL(10)	JET1323
	COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),	JET1324
1	TETAF(101),BF(101),	JET1325
2	XN(101),RMN(101),RPN(101),MN(101),MUN(101),	JET1326
3	TETAN(101),BN(101),XTEMP(101)	JET1327
	COMMON/THICKY/XTH(1002),TH(1002)	JET1328
	REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF	JET1329
	COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)	JET1330
1	,XIAPP(101,20),XIF(101,20)	JET1331
	COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,	JET1332
1	G16,G17,G18,G19,G20	JET1333
	COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,	JET1334
1	STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,	JET1335
2	TETSYM,TETLIM,DDY,DYMAX	JET1336
	COMMON /STAG/RH00,NO,P0,T0,A0,MDOT1	JET1337
	COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),	JET1338
1	RMCHARF(92),RPCARF(92),RMCARN(92),RPCARN(92),	JET1339
2	TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),	JET1340
3	CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),	JET1341
4	MCHARI(92)	JET1342
	COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,	JET1343
1	KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD	JET1344
	COMMON /ROW/YF,YN,DXF,DXN	JET1345
C	COMPUTE X-OPACITY.	JET1346
C	BEGIN FROM LIMITING CHARACTERISTIC OF AN ASSUMED P.M. FAN.	JET1347
C	XI0 -- THE THICKNESS BETWEEN THE LIMITING CHARACTERISTIC AND THE	JET1348
C	BOUNDARY CHARACTERISTIC OF THE NUMERICAL COMPUTATION.	JET1349
	DO 12 I=1,KF0	JET1350
	XIF(I,JXI)=XF(I)	JET1351
	XI(I,JXI)=0.	JET1352
	XIPM(I,JXI)=0.	JET1353
	XIGRP(I,JXI)=0.	JET1354
	XIAPP(I,JXI)=0.	JET1355
12	CONTINUE	JET1356
	IF(J.EQ.1) GO TO 1000	JET1357
	PSILIM=TETLIM	JET1358
	XLIM=XC+(YF-YC)/DTAN(PSILIM)	JET1359
	XBOUND=XF(KF)	JET1360
	KPM=10	JET1361
	DX=(XLIM-XBOUND)/DFLOAT(KPM)	JET1362
	SUM=0.	JET1363
	DO 1 I=1,KPM	JET1364
	X1=XBOUND+DFLOAT(I-1)*DX	JET1365
	X2=X1+DX	JET1366
	PS1=PAI2-DATAN((X1-XC)/(YF-YC))	JET1367
	PS2=PAI2-DATAN((X2-XC)/(YF-YC))	JET1368


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      Q1=(PS1-PSILIM)/G5
      Q2=(PS2-PSILIM)/G5
      IF(I.EQ.KPM) Q2=1.D-10
      IF(Q2.LT.0.) CALL FIN(1701)
      F1=G11*(DSIN(Q1))*((2.D0/(G-1.D0))
      F2=G11*(DSIN(Q2))*((2.D0/(G-1.D0))
      SUM=SUM+DX*(F1+F2)/2.D0
1     CONTINUE
      XI0=SUM*(NO*SIGMA)
C RE-EVALUATE XI0 FOR A RING-JET.
      IF(DELTA.EQ.0.) GO TO 14
      M=MFIN
      CALL MFUNC(M,F,ETA,TETA)
      PSI=TETA+DARSIN(1.D0/M)
      GOREM=1.D0+G1*M**2
      GOR=M**2-1.D0
      CALL HINTER(M,HM)
      DELTOB=0.5D0*DSQRT(GOR)*((1.D0/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1     +G15*HM/2.D0
      EVER=SIGMA*NO*YC/(M*DSIN(TETA)*DSIN(PSI)*GOREM**G6)
      GGG=2.D0-DELTOB*(G+1.D0)/2.D0
      IF(DABS(GGG).GT.1.D-10) GO TO 15
      PRINT 16, DELTOB,G,GGG
16  FORMAT(/1X,'FROM OPACX. GGG NEARLY ZERO. EXPRESSION FOR XI0 IS',
1     1X,'SINGULAR. DELTOB,G,GGG=',3D12.4/)
      CALL FIN(1715)
15  CONTINUE
      EVER=EVER/GGG
      XI0=EVER*((YF/YC)**GGG-1.D0)/(YF/YC)
14  CONTINUE
      XI(KF,JXI)=XI0
      XIPM(KF,JXI)=XI0
      XIGRP(KF,JXI)=XI0
      KF1=KF-1
      DO 2 II=1,KF1
      I=KF-II+1
      X1=XF(I)
      X2=XF(I-1)
      DX=X1-X2
      F1=1.D0/(1.D0+G1*MF(I)**2)**G6
      F2=1.D0/(1.D0+G1*MF(I-1)**2)**G6
      DTNUM=(NO*SIGMA)*DX*(F1+F2)/2.D0
      XI(I-1,JXI)=XI(I,JXI)+DTNUM
      XIPM(I-1,JXI)=1.D24
      XIGRP(I-1,JXI)=1.D24
      PS1=PAI2-DATAN((X1-XC)/(YF-YC))
      PS2=PAI2-DATAN((X2-XC)/(YF-YC))
      IF(PS2.GT.PSI1) GO TO 2
      Q1=(PS1-PSILIM)/G5
      Q2=(PS2-PSILIM)/G5
      IF(Q1.LT.0.) CALL FIN(1711)
      F1=G11*(DSIN(Q1))*((2.D0/(G-1.D0))
      F2=G11*(DSIN(Q2))*((2.D0/(G-1.D0))
      DTPM=(NO*SIGMA)*DX*(F1+F2)/2.D0
      XIPM(I-1,JXI)=XIPM(I,JXI)+DTPM
      DIST1=DSQRT((X1-XC)**2+(YF-YC)**2)
      DIST2=DSQRT((X2-XC)**2+(YF-YC)**2)
      KC1=KCLEAD+I-ILEAD
      KC2=KC1-1
      IF(KC2.LT.KCLEAD) GO TO 21
      M1=MCHARI(KC1)
      M2=MCHARI(KC2)
      CALL MATCH(I,M1,MG1,MOBI1,MABI1)
      CALL MATCH(I-1,M2,MG2,MOBI2,MABI2)
      F1=1.D0/(1.D0+G1*MG1**2)**G6
      F2=1.D0/(1.D0+G1*MG2**2)**G6
      DTGRP=(NO*SIGMA)*DX*(F1+F2)/2.D0
      XIGRP(I-1,JXI)=XIGRP(I,JXI)+DTGRP
21  CONTINUE
2  CONTINUE
C APPROXIMATE THICKNESS XIAPP(I,JXI). BASED ON CLOSED-FORM INTEGRATION.
      DO 3 I=1,KF

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XIAPP(I,JXI)=1.D24
KC=KCLEAD+(I-ILEAD)
IF(DELTA.EQ.0.) GO TO 3
IF(KC.LT.KCLEAD) GO TO 3
IF(XF(I).LT.XCHARF(1)) GO TO 3
M=MCHARI(KC)
CALL MFUNC(M,F,ETA,TETA)
PSI=TETA+DARSIN(1.D0/M)
GOREM=1.D0+G1*M**2
GOR=M**2-1.D0
CALL HINTER(M,HM)
DELTOB=0.5D0*DSQRT(GOR)*(1.D0/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1 +G15*HM/2.D0
EVER=SIGMA*N0*YC/(M*DSIN(TETA)*DSIN(PSI)*GOREM**G6)
GGG=2.D0-DELTOB*(G+1.D0)/2.D0
IF(DABS(GGG).GT.1.D-10) GO TO 25
PRINT 26, I,KC,M,DELTOB,G,GGG
26 FORMAT(/1X,'FROM OPACX. GGG NEARLY ZERO. EXPRESSION FOR XIO IS',
1 1X,'SINGULAR. I,KC,M=',I5,D12.4/
2 1X,'DELTOB,G,GGG=',3D12.4/)
CALL FIN(1725)
25 CONTINUE
EVER=EVER/GGG
XIAPP(I,JXI)=EVER*((YF/YC)**GGG-1.D0)/(YF/YC)
3 CONTINUE
1000 CONTINUE
RETURN
END
LOADC
SUBROUTINE LOADC
C SUBROUTINE NUMBER 18
IMPLICIT REAL*8(A-H,L-Z,$)
REAL*4 XPL,YPL
COMMON /PLUME/XPL(1002,10),YPL(1002)
COMMON /IPLUME/KPL,ITYPL(10)
COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1 TETAF(101),BF(101),
2 XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3 TETAN(101),BN(101),XTEMP(101)
COMMON/THICKY/XTH(1002),TH(1002)
REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF
COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20)
1 ,XIAPP(101,20),XIF(101,20)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1 G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1 STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2 TETSYM,TETLIM,DDY,DYMAX
COMMON /STAG/RH00,N0,P0,T0,A0,MDOT1
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1 KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
COMMON /ROW/YF,YN,DXF,DXN
COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92),
1 RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92),
2 TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92),
3 CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92),
4 MCHARI(92)
COMMON /ICHARA/KCHARP,KCHARM,KCHARO
C LOAD FLOW VARIABLES OF GRID POINTS IN THE FAN SEGMENT FROM THE
C SEMI-INVERSE INTEGRATION (IN SUBR. SEMINV). NOTE THAT GRID POINTS
C XN(I) WERE ALREADY DETERMINED IN SUBR. GRIDN.
DO 1 I=ILEAD,KN
KC=KCLEAD+I-ILEAD
IF(KC.GT.KCHARP) CALL FIN(1801)
RMN(I)=RMCARN(KC)
RPN(I)=RPCARN(KC)
MN(I)=MCHARN(KC)
MUN(I)=MUCARN(KC)
TETAN(I)=TCHARN(KC)
1 CONTINUE
RETURN
END
NUFUNC
DOUBLE PRECISION FUNCTION NUFUNC(M)

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C SUBROUTINE NUMBER 19 JET1513
  IMPLICIT REAL*8(A-H,L-Z,$) JET1514
  REAL*4 XPL,YPL JET1515
  COMMON /PLUME/XPL(1002,10),YPL(1002) JET1516
  COMMON /IPLUME/KPL,ITYPL(10) JET1517
  COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101), JET1518
1   TETAF(101),BF(101), JET1519
2   XN(101),RMN(101),RPN(101),MN(101),MUN(101), JET1520
3   TETAN(101),BN(101),XTEMP(101) JET1521
  COMMON/THICKY/XTH(1002),TH(1002) JET1522
  REAL*4 YXI,XI,XIPM,XIGRP,XIAPP,XIF JET1523
  COMMON /THICKX/YXI(20),XI(101,20),XIPM(101,20),XIGRP(101,20) JET1524
1   ,XIAPP(101,20),XIF(101,20) JET1525
  COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1526
1   G16,G17,G18,G19,G20 JET1527
  COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1528
1   STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET1529
2   TETSYM,TETLIM,DDY,DYMAX JET1530
  COMMON /STAG/RH00,NO,PO,TO,A0,MDOT1 JET1531
  COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET1532
1   KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET1533
  COMMON /ROW/YF,YN,DXF,DXN JET1534
  COMMON /CHARAC/XCHARF(92),YCHARF(92),XCHARN(92),YCHARN(92), JET1535
1   RMCARF(92),RPCARF(92),RMCARN(92),RPCARN(92), JET1536
2   TCHARF(92),TCHARN(92),MUCARF(92),MUCARN(92), JET1537
3   CSIGNN(92),CSIGNF(92),MCHARN(92),MCHARF(92), JET1538
4   MCHARI(92) JET1539
  COMMON /ICHARA/KCHARP,KCHARM,KCHARO JET1540
C COMPUTE NU AS FUNCTION OF MACH NUMBER M. NOTE THAT THE P.M. JET1541
C DEFINITION OF NU HAS BEEN MODIFIED BY ADDING A CONSTANT. THE USUAL JET1542
C CHOICE OF THE CONSTANT IS SUCH THAT NU=0 FOR INFINITE M. JET1543
  Q=1.DO/DSQRT(M**2-1.DO) JET1544
  NUFUNC=NUO-(G5*DATAN(G5*Q)-DATAN(Q)) JET1545
  RETURN JET1546
  END JET1547

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SUBROUTINE HMSET JET1548
C SUBROUTINE NUMBER 20 JET1549
  IMPLICIT REAL*8(A-H,L-Z,$) JET1550
  REAL*8 KAPA0B JET1551
  COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1552
1   G16,G17,G18,G19,G20 JET1553
  COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1554
1   STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO, JET1555
2   TETSYM,TETLIM,DDY,DYMAX JET1556
  COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET1557
1   KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD JET1558
  COMMON /GRP/DMINV,MHINV(101),HNV(101) JET1559
  COMMON /IGRP/KHM JET1560
C A ROUTINE FOR THE C+ DERIVATIVE DUE TO RING SYMMETRY (GRP). JET1561
  KHM=51 JET1562
  IF(KHM.GT.101) CALL FIN(2001) JET1563
  MINV0=1.DO/MEXIT JET1564
  DMINV=MINV0/DFLOAT(KHM-1) JET1565
  M=MEXIT JET1566
  SUM=0. JET1567
  KHM1=KHM-1 JET1568
  DO 1 I=1,KHM1 JET1569
  MF=M JET1570
  MHINV(I)=MINV0-DFLOAT(I-1)*DMINV JET1571
  M=1.DO/MHINV(I) JET1572
  DM=M-MF JET1573
  M1=M-DM JET1574
  M2=M-DM/2.DO JET1575
  M3=M JET1576
  CALL MFUNC(M1,F1,ETA1,TETA1) JET1577
  CALL MFUNC(M2,F2,ETA2,TETA2) JET1578
  CALL MFUNC(M3,F3,ETA3,TETA3) JET1579
  SUM=SUM+DM*(F1+4.DO*F2+F3)/6.DO JET1580
  ETA=ETA3 JET1581
  TETA=TETA3 JET1582
  PSI=TETA+DARSIN(1.DO/M) JET1583
  NORM=((3.DO-G)/4.DO)*(M**2-1.DO)**0.75DO/ JET1584

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HMSET

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1      (DSIN(PSI))*(1.D0+G1*M**2)**G14)
HM=SUM*NORM
HNV(I)=HM
GOREM=1.D0+G1*M**2
GOR=M**2-1.D0
DELTOB=0.5D0*DSQRT(GOR)*(1.D0/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1      +((G+1.D0)/(2.D0*(3.D0-G)))*HM
EPSIOB=DELTOB/DSQRT(GOR)-DSIN(TETA)/(M*DSIN(PSI))
KAPAOB=1.D0
IF(DABS(PIA2-TETA).GT.1.D-6)
1KAPAOB=DTAN(TETA)*EPSIOB
LAMDOB=EPSIOB-DELTOB*GOREM/(GOR*DSQRT(GOR))
PRINT 11,I,M,HM,TETA*DEG,PSI*DEG
11  FORMAT(1X,'      I,M,HM,TETA,PSI=',I5,5D12.4)
PRINT 12,DELTOB,EPSIOB*DEG,KAPAOB*DEG,LAMDOB*DEG
12  FORMAT(1X,'DELTOB,EPSIOB,KAPAOB,LAMDOB=',5X,5D12.4)
1  CONTINUE
MHINV(KHM)=0.
HNV(KHM)=1.D0
RETURN
END
MFUNC
SUBROUTINE MFUNC(M,F,ETA,TETA)
C  SUBROUTINE NUMBER 21
IMPLICIT REAL*8(A-H,L-Z,*)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1      G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2      NUPT1,TETLIM
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1      KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
COMMON /GRP/DMINV,MHINV(101),HNV(101)
C
NU=NUFUNC(M)
TETA=NUFUNC(MEXIT)+PAI2-NU
GOREM=1.D0+G1*M**2
GOR=M**2-1.D0
F=(M**2)*(GOREM**G13)*DSIN(TETA)/GOR**1.25D0
GOREM1=1.D0+G1*MEXIT**2
GOR1=MEXIT**2-1.D0
ETA=((GOREM/GOREM1)**G14)*((GOR1/GOR)**0.25D0)
RETURN
END
SUBROUTINE HINTER(M,H)
C  SUBROUTINE NUMBER 22
IMPLICIT REAL*8(A-H,L-Z,*)
COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1      G16,G17,G18,G19,G20
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NUO,
2      TETSYN,TETLIM,DDY,DYMAX
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1      KF2,IDEL,JDEL,JYXI,JXI,ILEAD,ILEADF,KCLEAD
COMMON /GRP/DMINV,MHINV(101),HNV(101)
COMMON /IGRP/KHM
C  COMPUTE H(M) BY INTERPOLATION
MINV=1.D0/M
I=KHM-IDINT(MINV/DMINV-1.D-9)-1
IF(I.GE.1.AND.I.LT.KHM) GO TO 1
PRINT 11,I,KHM,M,MEXIT
11  FORMAT(1X,'I,KHM,M,MEXIT=',2I5,2D14.6/)
CALL FIN(2201)
1  CONTINUE
F1=(MINV-MHINV(I+1))/DMINV
F2=1.D0-F1
IF(F1.LT.-1.D-9) CALL FIN(2210)
IF(F2.LT.-1.D-9) CALL FIN(2211)
H=F1*HNV(I)+F2*HNV(I+1)
RETURN
END
MATCH
SUBROUTINE MATCH(I,MOB,MAB,MOBI,MABI)
C  SUBROUTINE NUMBER 23

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      IMPLICIT REAL*8(A-H,L-Z,*)
      COMMON /VECS/XF(101),RMF(101),RPF(101),MF(101),MUF(101),
1      TETAF(101),BF(101),
2      XN(101),RMN(101),RPN(101),MN(101),MUN(101),
3      TETAN(101),BN(101),XTEMP(101)
      COMMON /ROW/YF,YN,DXF,DXN
      COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15,
1      G16,G17,G18,G19,G20
      COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT,
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0,
2      TETSYM,TETLIM,DDY,DYMAX
      COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J,
1      KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD
      COMMON /GRP/DMINV,MHINV(101),HNV(101)
      COMMON /IGRP/KHM
C COMPUTE H(M) AND THE ALFA-DERIVATIVES
      M=MOB
      CALL MFUNC(M,F,ETA,TETA)
      PSI=TETA+DARSIN(1.D0/M)
      CALL HINTER(M,HM)
      GOREM=1.D0+G1*M**2
      GOR=M**2-1.D0
      DELTOB=0.5D0*DSQRT(GOR)*(1.D0/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1      +G15*HM/2.D0
      FOB=(G7*GOREM)**G2/M
      FAB=FOB*(YF/YC)**DELTOB
      CALL AREAFA(FAB,MAB)
C COMPUTE MABI FROM THE INVERSE PROBLEM SOLUTION
      COTAV=(XF(I)-XC)/(YF-YC)
      PSI0=PAI2-DATAN(COTAV)
      EVY=YF*DLOG(YF/YC)/(YF-YC)-1.D0
      PSIN=PSI0
      DO 1 ITER=1,50
      PSI=PSIN
      M=DSQRT(1.D0+G4/DTAN((PSI-TETLIM)/G5)**2)
      M=DMAX1(M,MEXIT)
      CALL HINTER(M,HM)
      CALL MFUNC(M,F,ETA,TETA)
      GOREM=1.D0+G1*M**2
      GOR=M**2-1.D0
      DELTOB=0.5D0*DSQRT(GOR)*(1.D0/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1      +G15*HM/2.D0
      EPSIOB=DELTOB/DSQRT(GOR)-DSIN(TETA)/(M*DSIN(PSI))
      LAMDOB=EPSIOB-DELTOB*GOREM/(GOR*DSQRT(GOR))
      COTN=COTAV+LAMDOB*EVY/DSIN(PSI)**2
      PSIN=PAI2-DATAN(COTN)
      DPSI=PSIN-PSI
      IF(DABS(DPSI).LT.1.D-9) GO TO 11
1      CONTINUE
      PRINT 12,I,ITER,PSI,PSIN,DPSI,M,XF(I),YF,XC,YC
12      FORMAT(/1X,'I,ITER,PSI,PSIN,DPSI,M,XF(I),YF,XC,YC='//
1      1X,2I4,8D11.3/)
      CALL FIN(2301)
11      CONTINUE
C USING MOBI=M AS COMPUTED FROM THE INVERSE PROBLEM, FIND MABI.
      MOBI=M
      M=MOBI
      CALL MFUNC(M,F,ETA,TETA)
      PSI=TETA+DARSIN(1.D0/M)
      CALL HINTER(M,HM)
      GOREM=1.D0+G1*M**2
      GOR=M**2-1.D0
      DELTOB=0.5D0*DSQRT(GOR)*(1.D0/(MEXIT*ETA)+DSIN(TETA)/M)/DSIN(PSI)
1      +G15*HM/2.D0
      FOB=(G7*GOREM)**G2/M
      FAB=FOB*(YF/YC)**DELTOB
      CALL AREAFA(FAB,MABI)
      RETURN
      END
      SUBROUTINE AREAFA(F,M)
C SUBROUTINE NUMBER 24
      IMPLICIT REAL*8(A-H,L-Z,*)

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AREAFA

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COMMON /GAMA/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11,G12,G13,G14,G15, JET1729
1      G16,G17,G18,G19,G20 JET1730
COMMON /PAR/PAI,PAI2,DEG,XC,YC,MEXIT,MFIN,YMAX,DY0,DY,DYNEXT, JET1731
1      STAB,DELTA,PSI1,PSIF,ZETA1,SIGMA,FRACG,EPSIL,NU0, JET1732
2      TETSYM,TETLIM,DDY,DYMAX JET1733
COMMON /IPAR/JMAX,KF0,ITER0,KF,KN,IM,IP,J, JET1734
1      KF2,IDEL,JDEL,JYXI,JXI,Ilead,Ileadf,KCLEAD JET1735
COMMON /GRP/DMINV,MHINV(101),HNV(101) JET1736
COMMON /IGRP/KHM JET1737
C COMPUTE MACH NUMBER M FROM AREA RATIO FUNCTION F JET1738
C  $F = ((2/(G+1)) * (1 + (G-1) * M ** 2)) ** ((G+1)/(2*(G-1))) / M$  JET1739
C INITIAL GUESS IS MIN JET1740
E1=(F*MEXIT)**(1.D0/G2)/G7 JET1741
E2=(E1-1.D0)/G1 JET1742
E3=DMAX1(E2,MEXIT**2) JET1743
MIN=DSQRT(E3) JET1744
EMN=MIN JET1745
DO 1 I=1,100 JET1746
EMO=EMN JET1747
GOREM=1.D0+G1*EMO**2 JET1748
GOR=EMO**2-1.D0 JET1749
FO=(G7*GOREM)**G2/EMO JET1750
DF=FO-F JET1751
C PRINT 123,I,EMO,EMN,FO,F,DF,GOR,GOREM JET1752
C123 FORMAT(1X,'I,EMO,EMN,FO,F,DF,GOR,GOREM=',I5,7D12.4) JET1753
DFDM=FO*GOR/(EMO*GOREM) JET1754
DMN=DF/DFDM JET1755
EMN=EMO-DMN JET1756
EPSEM=DABS(DMN/EMN) JET1757
IF(EPSEM.LT.1.D-10) GO TO 11 JET1758
1 CONTINUE JET1759
CALL FIN(2401) JET1760
11 CONTINUE JET1761
M=EMN JET1762
RETURN JET1763
END JET1764

```

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